

Ultra-high energy neutrinos from the atmosphere and the cosmos

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Overview

- Atmospheric neutrinos:
 - New calculation of the prompt neutrino flux
- Neutrinos from astrophysical sources:
 - Introduction to GRBs and other sources
 - Neutrinos from charm production \Rightarrow prompt flux
- Based on work with M.H. Reno and I. Sarcevic

[arXiv:0806.0418 and arXiv:0808.2807, in PRD]

Cosmic neutrinos

- Neutrino background ($1.9 \text{ K} \rightarrow 10^{-4} \text{ eV}$)
- Solar neutrinos (MeV)
- Supernova neutrinos (MeV)
- **Atmospheric neutrinos** (up to 10^8 – 10^9 GeV)
- **Galactic / extragalactic neutrinos** (GeV to EeV)

(GZK, AGNs, GRBs, SNe with jets, other astrophysical sources etc...)
- **New physics** (e.g. dark matter annihilation)

Neutrinos as probes

- Escape from extreme environments
- Not deflected by magnetic fields, so point back to source
- Probe particle production in astrophysical sources
- Much higher energies than available in colliders
- Experiments: IceCube, Antares, KM3NeT, etc...

Atmospheric and extragalactic

- I will talk about two processes that generate high energy neutrinos:
 - Atmospheric interactions of cosmic rays
 - Astrophysical sources (SNe, GRBs, etc.)
- Common theme:
 - Hadronic or photo-hadronic collisions produce hadrons, some of which decay to neutrinos
- Example: $pp \rightarrow \pi^+ + X$

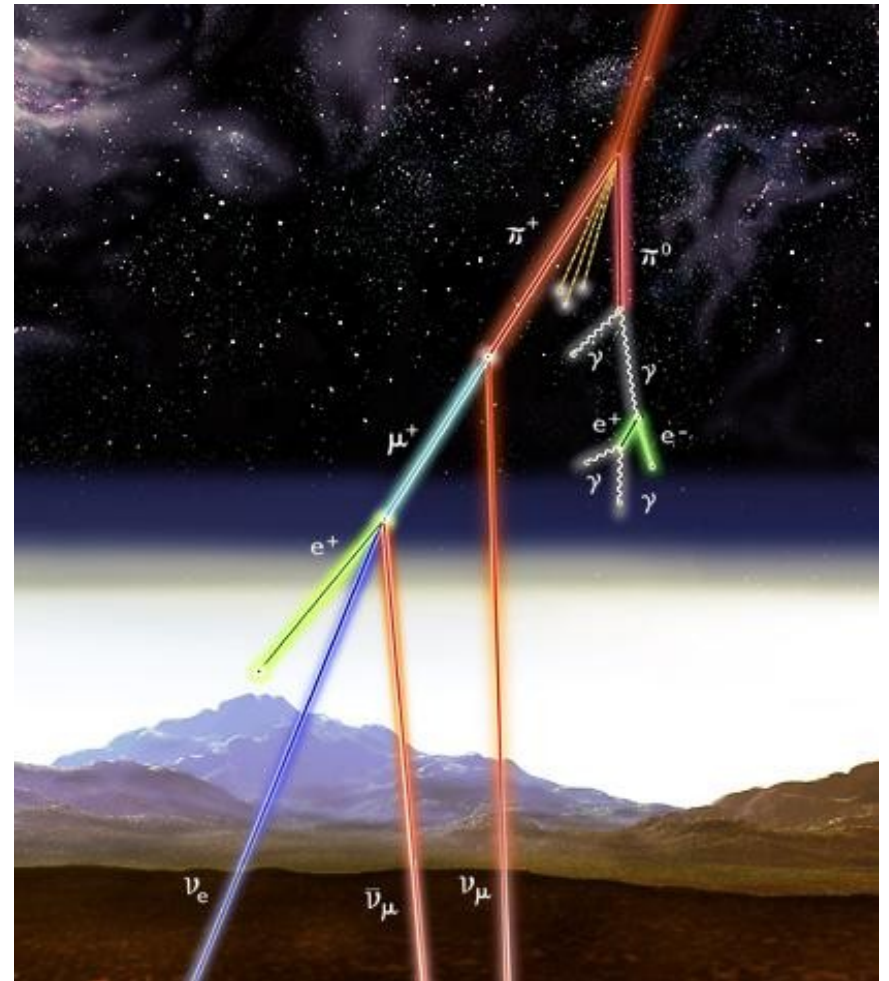
$$\pi^+ \rightarrow \mu^+ \nu_{\mu}$$

$$\mu^+ \rightarrow \bar{\nu}_{\mu} \nu_e e^+$$

Atmospheric neutrinos

Atmospheric neutrinos

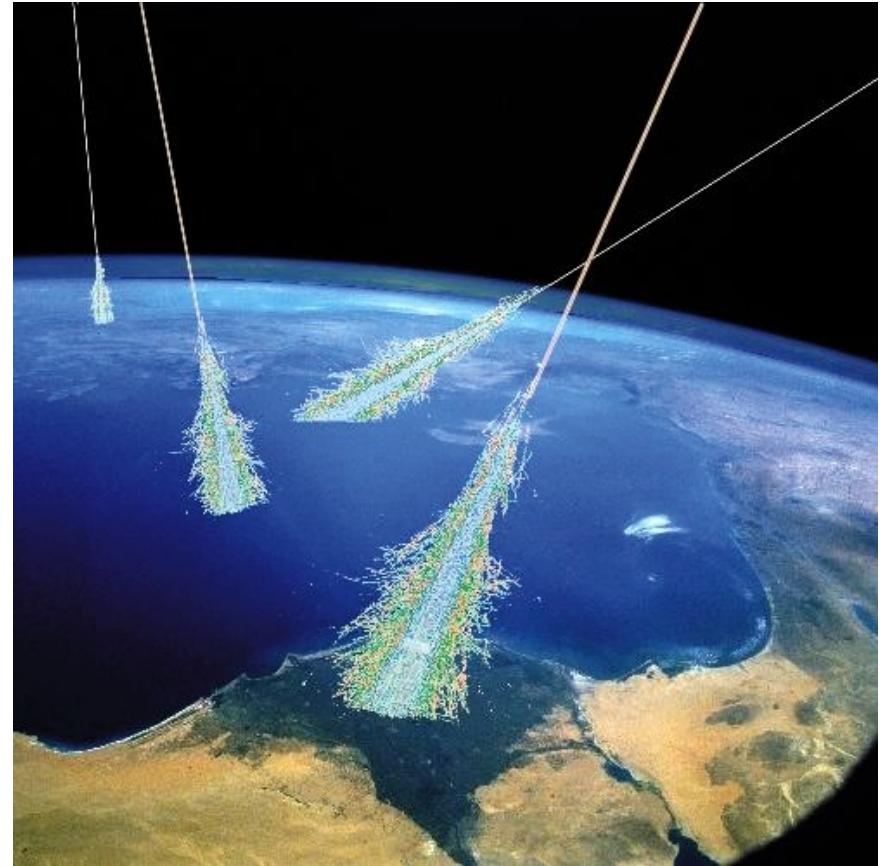
- Cosmic rays bombard upper atmosphere and collide with air nuclei
- CMS energy is large
⇒ secondary hadrons: pions, kaons, D-mesons ...
- Secondary particles interact and decay
⇒ cascade of particles



Credit: INFN-Notizie No.1 June 1999

Atmospheric neutrinos

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Credit: Astropic of the day, 060814

Why are we interested?

- Atmospheric neutrinos are a background to extragalactic neutrinos
- They are a test beam for neutrino experiments
- Can learn about cascades and the underlying production mechanism
- Higher energy pp collisions than in LHC:
can maybe even learn something about QCD

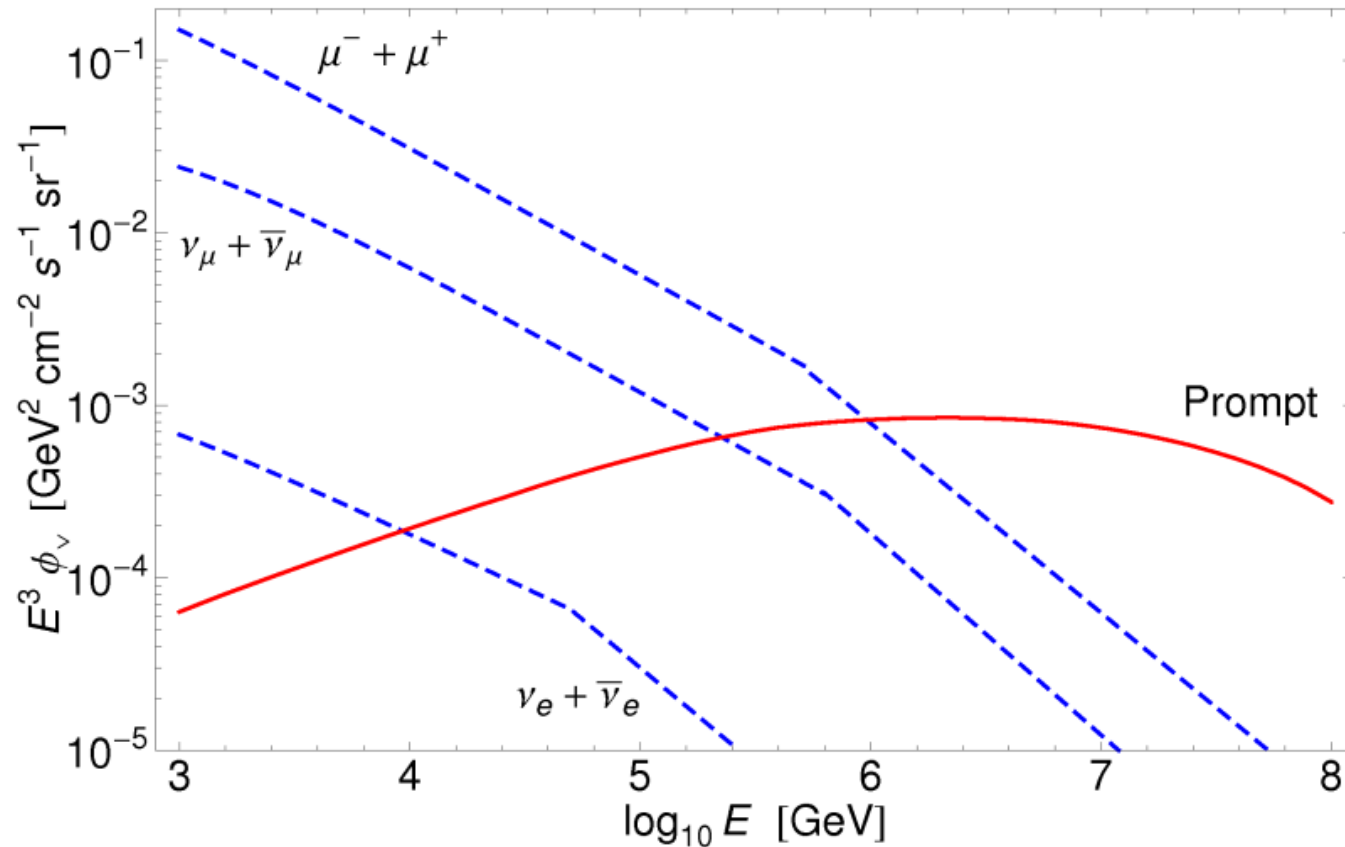
Conventional neutrino flux

- Pions and kaons are produced in more or less every inelastic collision
- π^+ always decays to neutrinos ($\pi^+ \rightarrow \mu^+ \nu_\mu$ is 99.98 %)
- *But π , K are long-lived* ($c\tau \sim 8$ meters for π^+)
 - ⇒ lose energy through hadronic collisions before decaying
 - ⇒ neutrino energies are degraded
- This is called the *conventional neutrino flux*

Prompt neutrino flux

- Hadrons containing heavy quarks (*charm or bottom*) are extremely short-lived:
 - ⇒ decay before losing much energy
 - ⇒ neutrino energy spectrum is harder
- However, production cross-section is much smaller
- But it turns out that there is a cross-over energy above which prompt neutrinos dominate over the conventional flux
- This is called the *prompt neutrino flux*

Prompt vs conventional fluxes



Prompt flux: RE, M.H. Reno, I. Sarcevic, arXiv:0806.0418

Conventional: Gaisser & Honda, Ann. Rev. Nucl. Part. Sci. **52**, 153 (2002)

All three lepton flavors are approximately equal for prompt flux

Prompt flux calculation

- Prompt fluxes have been calculated years ago using various phenomenological models of the charm production mechanism
- Thunman, Ingelman, Gondolo [[Astropart. Phys. 5, 309 \(1996\)](#)] did the first “real” QCD calculation
- Used **LO perturbative QCD** (in PYTHIA) and Monte Carlo-simulated the cascade
- Extended to **NLO QCD** by Pasquali, Reno, Sarcevic

Problem with QCD

- Charm cross section in QCD:

$$\frac{d\sigma_{\text{LO}}}{dx_F} = \int \frac{dM_{c\bar{c}}^2}{(x_1 + x_2)s} \sigma_{gg \rightarrow c\bar{c}}(\hat{s}) G(x_1, \mu^2) G(x_2, \mu^2)$$

where

$$x_{1,2} = \frac{1}{2} \left(\sqrt{x_F^2 + \frac{4M_{c\bar{c}}^2}{s}} \pm x_F \right)$$

- CMS energy is **large**
- Thus at large energy, **$x_1 \sim x_F$** and **$x_2 \ll 1$**

Problem with QCD

- In this case, fixed order QCD (LO or NLO) does not work well – there are large logarithms that must be resummed:

$$[\alpha_s \log(1/x)]^n$$

- Parton distribution functions poorly known at small x
- If logs are resummed (*BFKL equation*) one finds power growth of gluon distribution as $x \rightarrow 0$
- It grows so large that ultimately unitarity would be violated (T-matrix > 1)

Parton saturation

- Unitarity is saved through a phenomenon known as *saturation*:
 - The number of gluons in the nucleon becomes so large that gluons start interacting
 - Leads to a reduction in the growth
 - Non-linear parton evolution equations
- This is sometimes called the *color glass condensate*
- The simplest evolution equation is the *Balitsky–Kovchegov equation*: BFKL with non-linear term

Charm production

- We calculate the differential charm production cross section $d\sigma/dx_F$
- To include the effects of parton saturation, calculation is done in *dipole picture*, using an approximate solution of the Balitsky–Kovchegov equation
- This suppresses the cross section at larger energy relative to NLO QCD

Cascade equations

- To find the neutrino flux we must then solve the cascade equations given the incoming proton flux:

$$\frac{d\phi_N}{dX} = -\frac{\phi_N}{\lambda_N} + S(NA \rightarrow NY)$$

$$\frac{d\phi_M}{dX} = S(NA \rightarrow MY) - \frac{\phi_M}{\rho d_M(E)} - \frac{\phi_M}{\lambda_M} + S(MA \rightarrow MY)$$

$$\frac{d\phi_\ell}{dX} = \sum_M S(M \rightarrow \ell Y)$$

- X is the slant depth: “amount of atmosphere”
 ρd_M is the decay length, with ρ the density of air
 λ_M is the interaction length for hadronic energy loss

The atmosphere

- The distance traveled in the atmosphere is measured by the slant depth:

$$X(\ell, \theta) = \int_{\ell}^{\infty} d\ell' \rho(h(\ell', \theta)),$$

where $\rho(h) = \rho_0 \exp(-h/h_0)$

and $h_0 = 6.4 \text{ km}$

$$\rho_0 = 2.03 \times 10^{-3} \text{ g/cm}^3$$

- The total vertical depth $X \simeq 1300 \text{ g/cm}^3$
and horizontal $X \simeq 36,000 \text{ g/cm}^3$
- The atmosphere consists of “air nuclei” with $A=14.5$

The incoming proton flux

- We assume the incoming flux is protons, with a flux with a knee given by

$$\phi_N(E) = \begin{cases} 1.7 E^{-2.7} & \text{for } E < 5 \cdot 10^6 \text{ GeV} \\ 174 E^{-3} & \text{for } E > 5 \cdot 10^6 \text{ GeV} \end{cases}$$

- To good approximation it is isotropic at high energy

Particle production

The regeneration function is defined by

$$S(k \rightarrow j) = \int_{E_j}^{\infty} dE_k \frac{\phi_k(E_k)}{\lambda_k(E_k)} \frac{dn(k \rightarrow j; E_k, E_j)}{dE_j}.$$

where $dn/dE = (1/\sigma) d\sigma/dE$.

Describes energy distribution of produced particles

Z-moments

- We solve the cascade equations by introducing Z-moments:

$$Z_{kh} = \int_E^\infty dE' \frac{\phi_k(E', X, \theta)}{\phi_k(E, X, \theta)} \frac{\lambda_k(E)}{\lambda_k(E')} \frac{dn(kA \rightarrow hY; E', E)}{dE}$$

- Then

$$\frac{d\phi_M}{dX} = -\frac{\phi_M}{\rho d_M} - \frac{\phi_M}{\lambda_M} + Z_{MM} \frac{\phi_M}{\lambda_M} + Z_{NM} \frac{\phi_N}{\lambda_N}$$

- Solve equations separately in low- and high-energy regimes where attenuation is dominated by decay and energy loss, respectively, and interpolate

Lepton fluxes

- This gives

$$\phi_\ell^{\text{low}} = Z_{M\ell, \gamma+1} \frac{Z_{NM}}{1 - Z_{NN}} \phi_N(E)$$

$$\phi_\ell^{\text{high}} = Z_{M\ell, \gamma+2} \frac{Z_{NM}}{1 - Z_{NN}} \frac{\ln(\Lambda_M / \Lambda_N) \epsilon_M}{1 - \Lambda_N / \Lambda_M} \frac{\epsilon_M}{E} \phi_N(E),$$

where ϵ_M separates low and high energy regions:

$$\epsilon_M(\theta) = \frac{m_M c^2 h_0}{c \tau_M} f(\theta)$$

For small angles (near vertical): $f(\theta) = 1 / \cos \theta$

- We include charmed hadrons $M = D^\pm, D^0, \bar{D}^0, D_s^\pm, \Lambda_c^\pm$

Attenuation lengths

- Interaction (cooling) length for particle N is given by

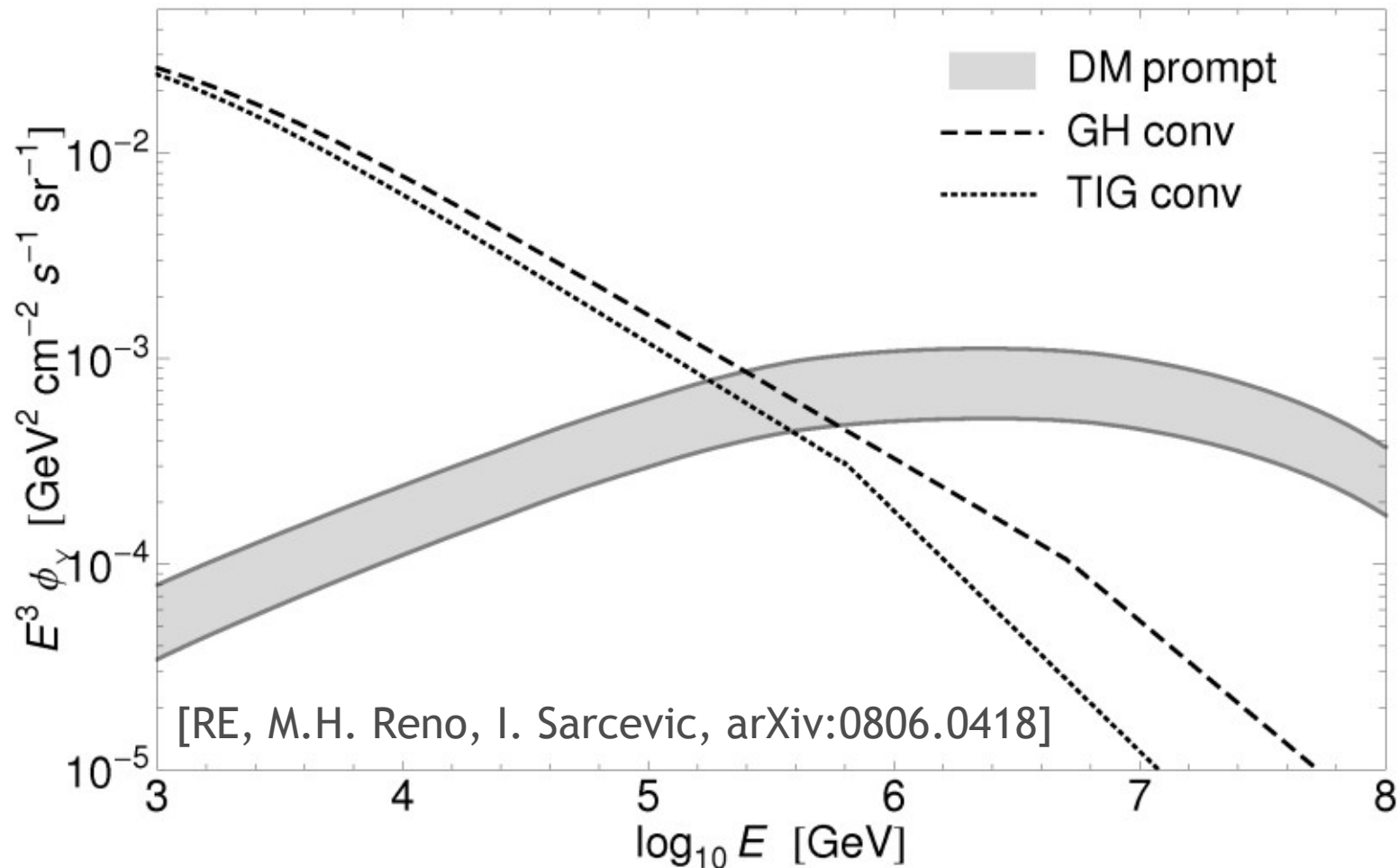
$$\lambda_N(E) = \frac{\rho(h)}{\sigma_{NA}(E)n_A(h)}$$

- Attenuation length is defined as

$$\Lambda_N(E) = \frac{\lambda_N(E)}{1 - Z_{NN}(E)}$$

where $(1 - Z_{NN})$ takes the energy loss in each interaction into account

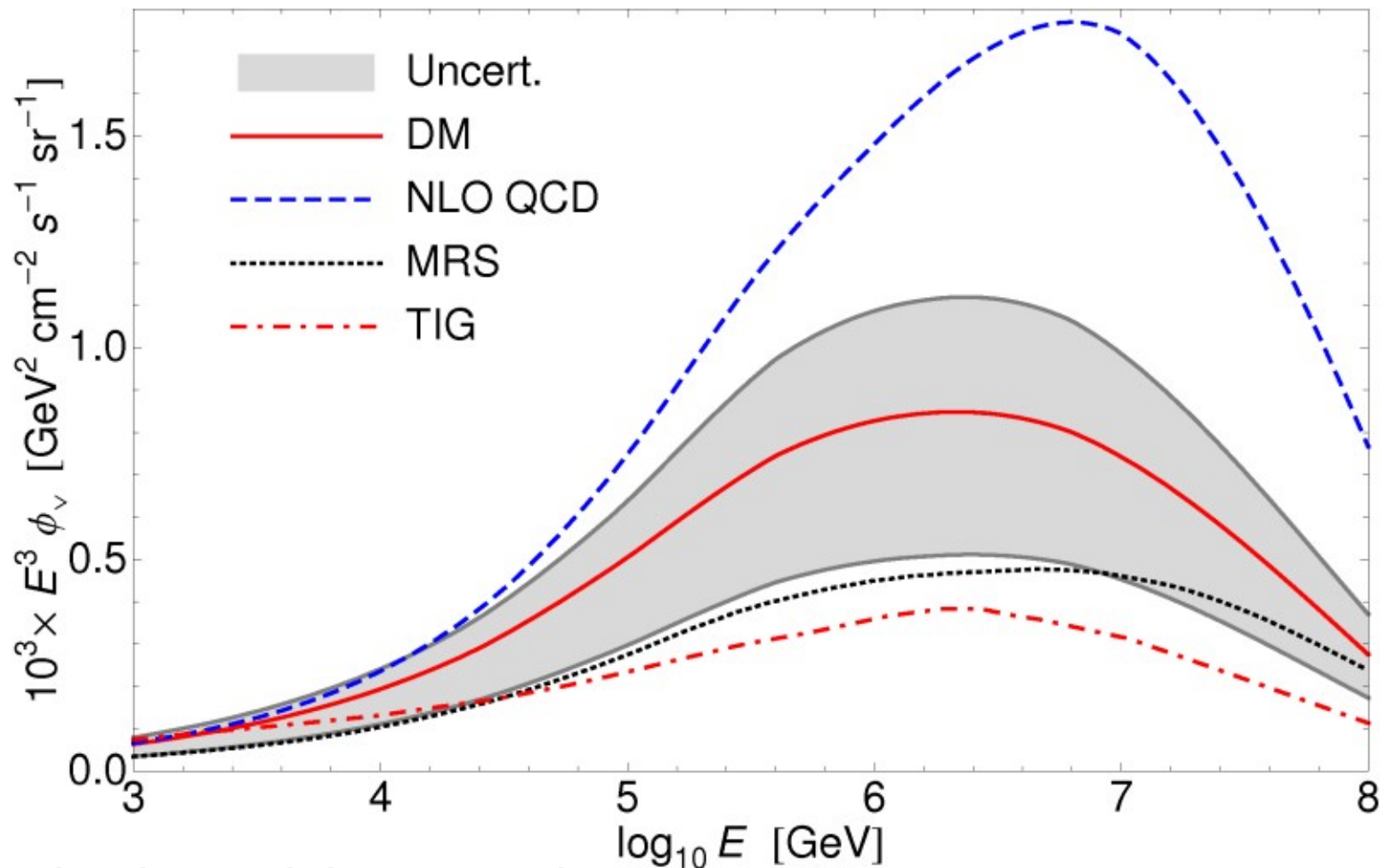
Best result for ν_μ



Uncertainty: gluon distribution, charm mass, factorization scale, parameters in saturation calculation

Prompt flux crosses over at $10^5 - 10^{5.5}$ GeV

Comparison: earlier calculations



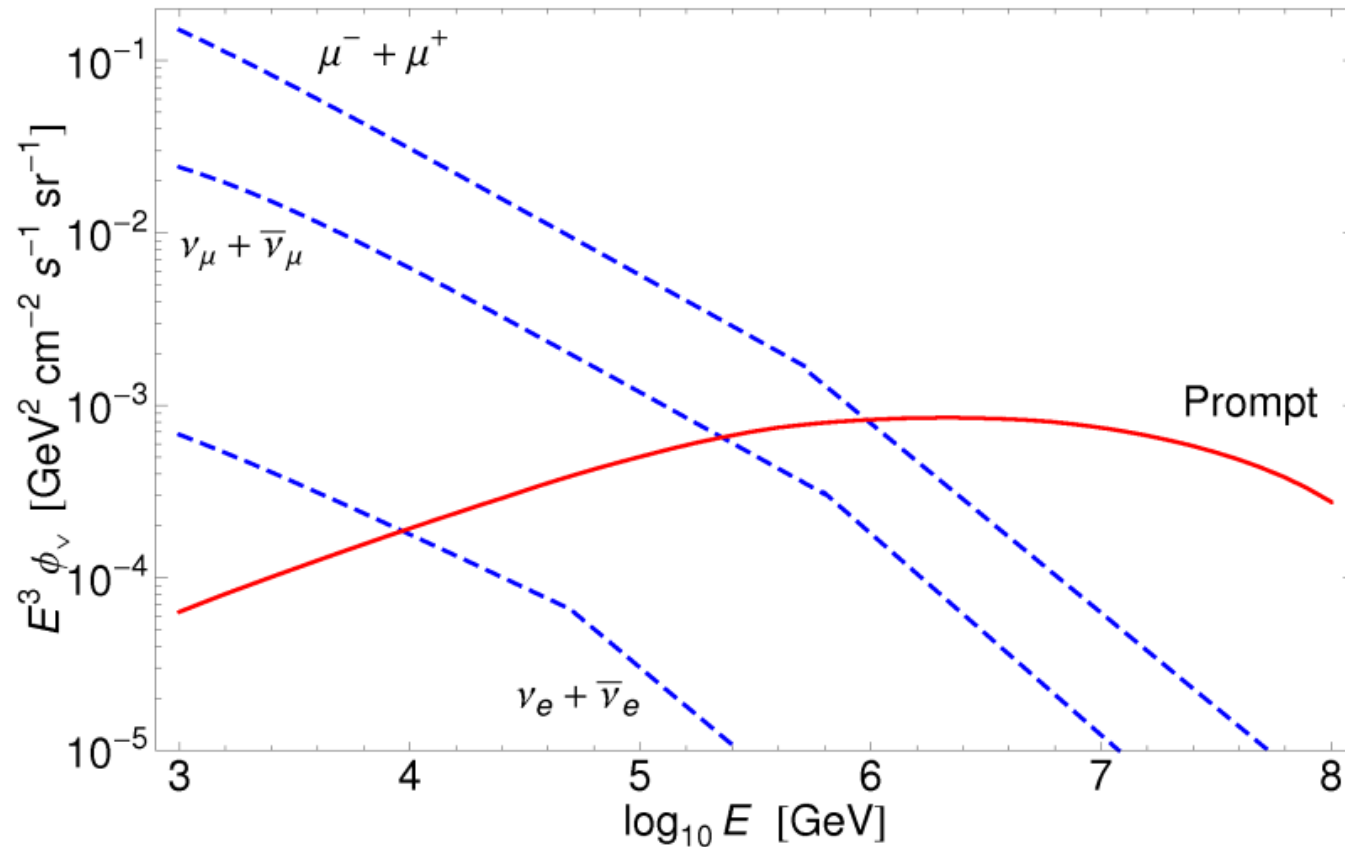
DM: dipole model — our calc.

NLO QCD: Pasquali, Reno, Sarcevic

MRS: Martin, Ryskin, Stasto (*included simpler saturation pheno.*)

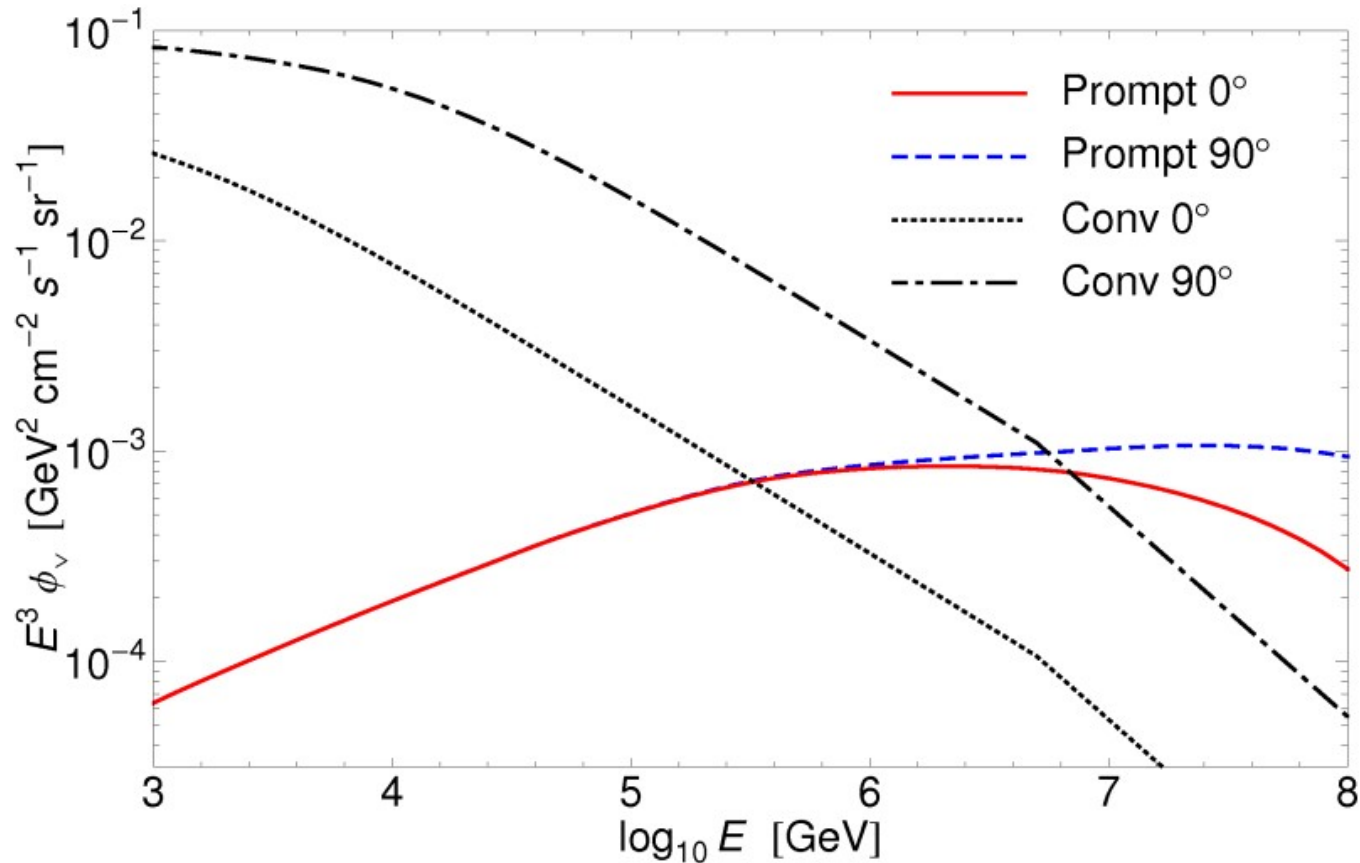
TIG: Thunman, Ingelman, Gondolo

Prompt vs conventional fluxes



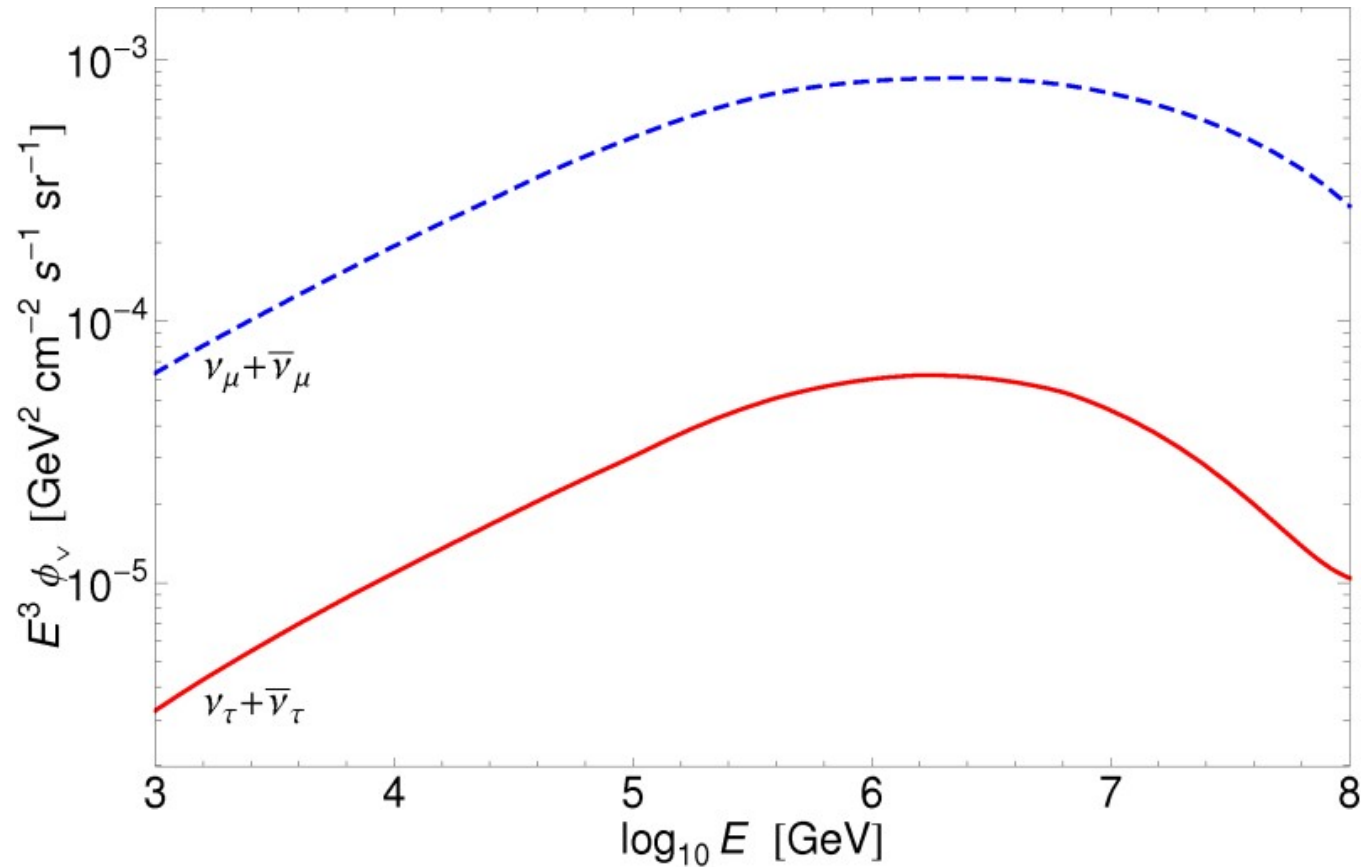
- Conventional flux different for different flavors
 - ν_e would be good for studying prompt flux

Zenith angle dependence



To see the prompt flux we want to look in the **vertical direction**

Tau neutrinos



Only D_s decays give tau neutrinos

***Gamma ray bursts and
astrophysical sources***

Charm in astrophysical sources

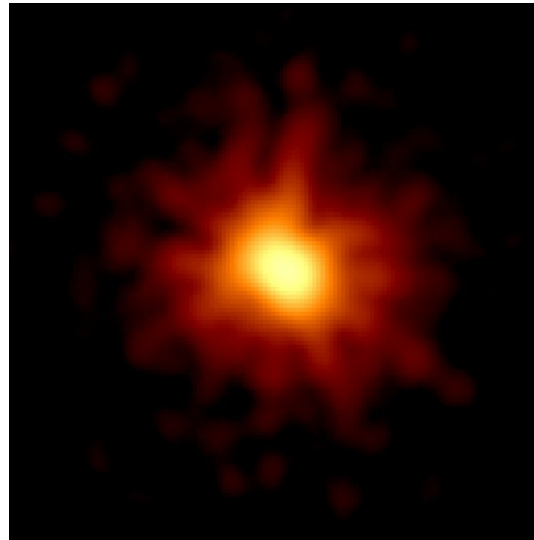
- We saw that for atmospheric neutrinos, charm dominates at high energies because D-mesons decay before they lose energy through hadronic interactions
- Obvious question: what about charm in astrophysical sources? Not usually taken into account.
- We'll see that then electromagnetic energy loss is more important, but the overall result is similar

Gamma ray bursts

- Gamma Ray Bursts (GRBs) are the most violent phenomena observed in the universe
- Energy output in 10 sec:
 - ~ 10^{53} – 10^{54} **ergs** isotropic energy equivalent
 - ~ 10^{51} – 10^{52} ergs if emission is ***jetted*** ($\theta \sim 5^\circ$)
- Supernovae emit a similar amount of energy during several months
- About one GRB per day is observed

Biggest burst: GRB 080319B

- GRB 080319B ($z = 0.94$) was the most distant object ever observed that could have been seen with the naked eye



- Above picture is in X-ray
- More than a million times brighter than SN 2005ap
- Unclear why so bright: maybe jet was head on

Gamma ray bursts

- Cosmological distances – observed up to $z = 6-7$
 $z=7$ means the universe was less than a billion years old!
- There are two classes of GRBs:
 - *Long*: ($t > 2$ s) occur in star-forming regions
 - *Short*: ($t < 2$ s) occur anywhere
- Long-duration bursts can be used as probe of star formation rates
- Not good standard candles for cosmology

What are GRBs ?

Probably short and long GRBs are of different origin;
both involve formation of a black hole

- **Short bursts** are believed to be binary mergers:
NS-NS or NS-BH
- **Long bursts** are believed to be core-collapse SNe
(e.g. Wolf-Rayet stars, type Ic)

There is observational evidence for the latter:
SNe seen at GRB sites

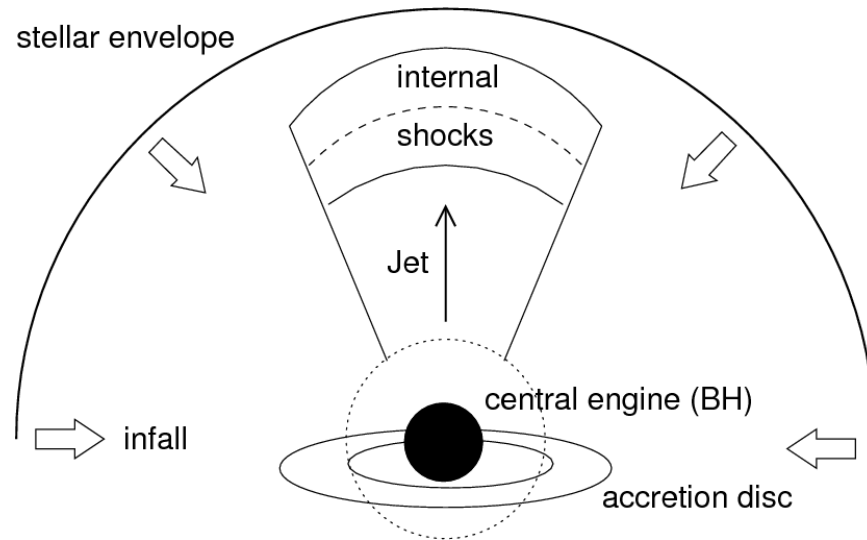
(e.g. GRB 980425 and SN 1998bw)

What are GRBs ?

Standard interpretation:

- GRBs are related to births of black holes
- The central engine releases a huge amount of energy in a small region
- This creates a very dense fireball
- Fireball expands due to trapped radiation pressure
- Relativistic outflow in two opposite **jets**
- The burst of gamma rays comes from dissipation in the outflow due to shocks
 - **synchrotron emission** and **inverse Compton**

Schematic picture



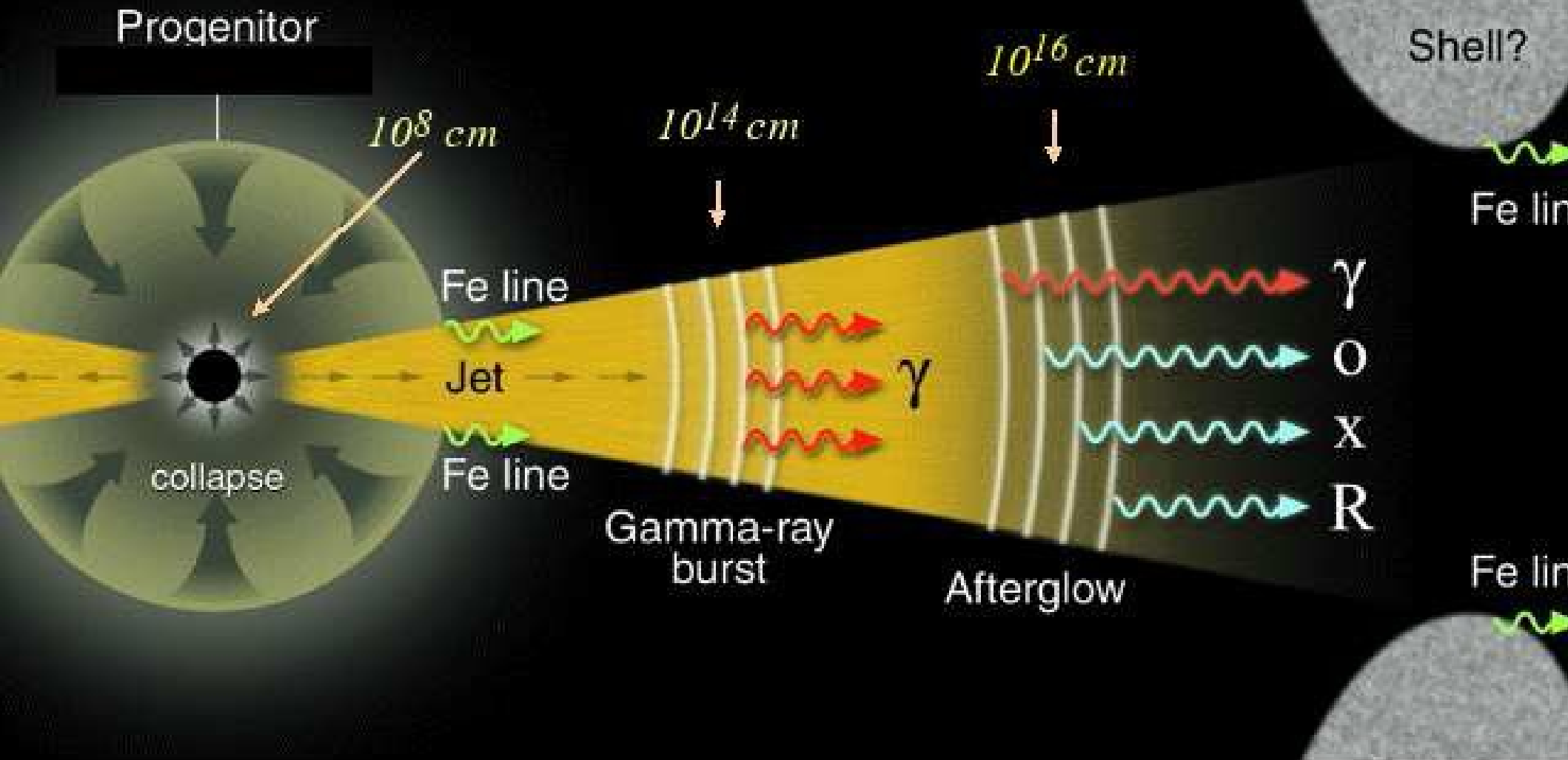
Relativistic jet inside a collapsing star – may or may not punch through the envelope

Protons and electrons are shock accelerated in jet

There are many similar types of astrophysical sources with jets:

- Active Galactic Nuclei (*jets from supermassive black hole*)
- Supernovae with jets (*slower jets, halted in star*)
- Microquasars

Anatomy of a GRB



See Piran 1999; Mészáros 2002 (ARAA) for reviews

Type Ic supernovae and GRBs

GRBs connected to core-collapse supernovae ?

Animation shows a Wolf-Rayet star of mass $M \sim 10 M_{\odot}$ exploding due to a GRB

- Core collapses to black hole \Rightarrow **fireball & jet**
- Jet protrudes and blows up the star \Rightarrow **SN Type Ic**

Type Ic supernovae and GRBs

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Acceleration and emission

- There are internal shocks in the jet
- Electrons and protons are shock accelerated to very high energy through the *Fermi mechanism*
- Electrons cool down through synchrotron emission in magnetic field
- If optically thin environment: gamma rays escape and make up the burst
- If optically thick: photons can thermalize
- Bulk Lorentz factor of jet must be $\gtrsim 100$ to obtain optical thin system

***Neutrinos from
astrophysical sources***

Cosmic beam dump

- Shock accelerated protons may collide with protons and photons in the jet and the star
- Mesons produced in collisions decay to γ and ν
- Waxman & Bahcall (1997) considered high energy neutrino flux from pions produced in GRBs – many authors have considered π and K in various sources (Ando-Beacom, Mészáros-Razzaque-Waxman, Koers-Wijers, many others)
- Pions, kaons are cooled before decay
– charmed mesons will persist to higher energies

Astrophysical sources

We consider two kinds of sources as examples:

- GRB:
 - Non-thermal photons and highly relativistic jet
- “Slow-jet supernova” (SJS):
 - Supernova with mildly relativistic jet that doesn't punch through
 - Thermal photons
 - SNe with jets may be common and may help with blowing up the star

(Razzaque, Meszaros, Waxman; Ando and Beacom)

Parameters

Calculation or obs, with $L_j = 3 \times 10^{50}$ erg/s :

Source	Γ_j	n'_p [cm^{-3}]	B' [G]	E'_γ [keV]	n'_γ [cm^{-3}]
SJS	3	4×10^{20}	10^9	4.5	3×10^{24}
GRB	100	3×10^{16}	10^7	2.5	1×10^{21}

We calculate the neutrino fluxes for these two toy-model sources

To do this, we need to take proton and meson cooling into account

Cooling

- Time scales for cooling of protons and mesons are

$$t'_{\text{cool}} = \frac{E'}{|dE'/dt'|}$$

with

$$|dE'/dt'| \simeq n' \sigma v \Delta E$$

- For photons, we use $|dE'/dt'| \simeq \langle n' \sigma v \rangle \Delta E$,
averaged over the photon distribution

Hadronic cooling

- pp and $p\gamma$ interactions as well as synchrotron and inverse Compton cool the accelerated protons
- Roughly, the cooling time scales are

$$t'_{p\gamma} = \frac{E'_p}{c\sigma_{p\gamma}n'_\gamma\Delta E'_p} \quad t'_{pp} = \frac{E'_p}{c\sigma_{pp}n'_p\Delta E'_p}$$

- For photons,

$$\langle n'\sigma v \rangle = \frac{c}{8\beta'_p E_p'^2} \int dE'_\gamma \frac{\hat{n}_\gamma(E'_\gamma)}{E_\gamma'^2} \int ds (s - m_p^2) \sigma_{p\gamma}(s)$$

Electromagnetic cooling & decay

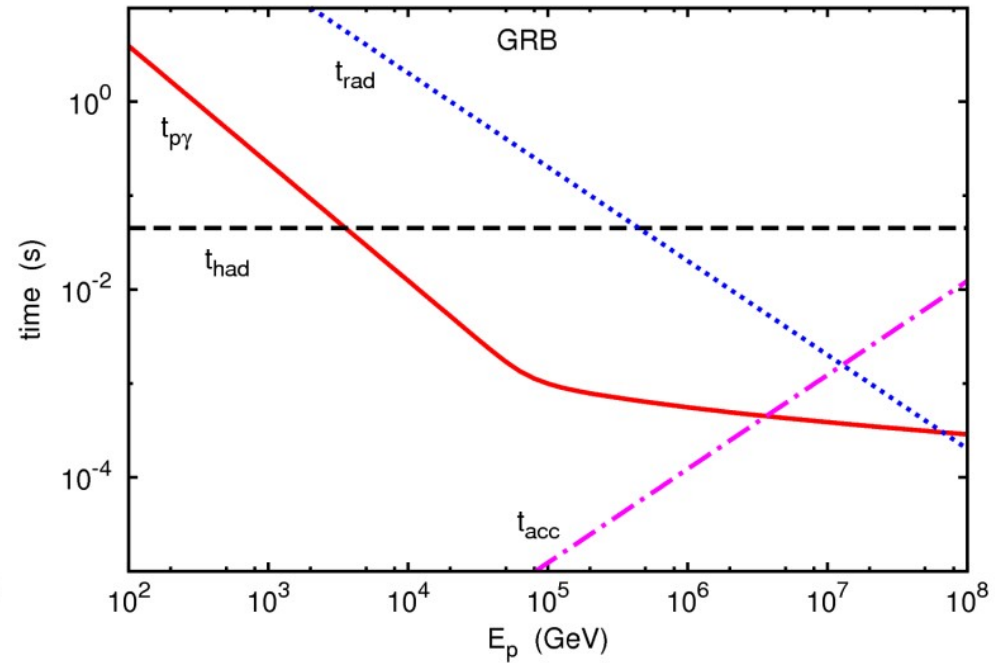
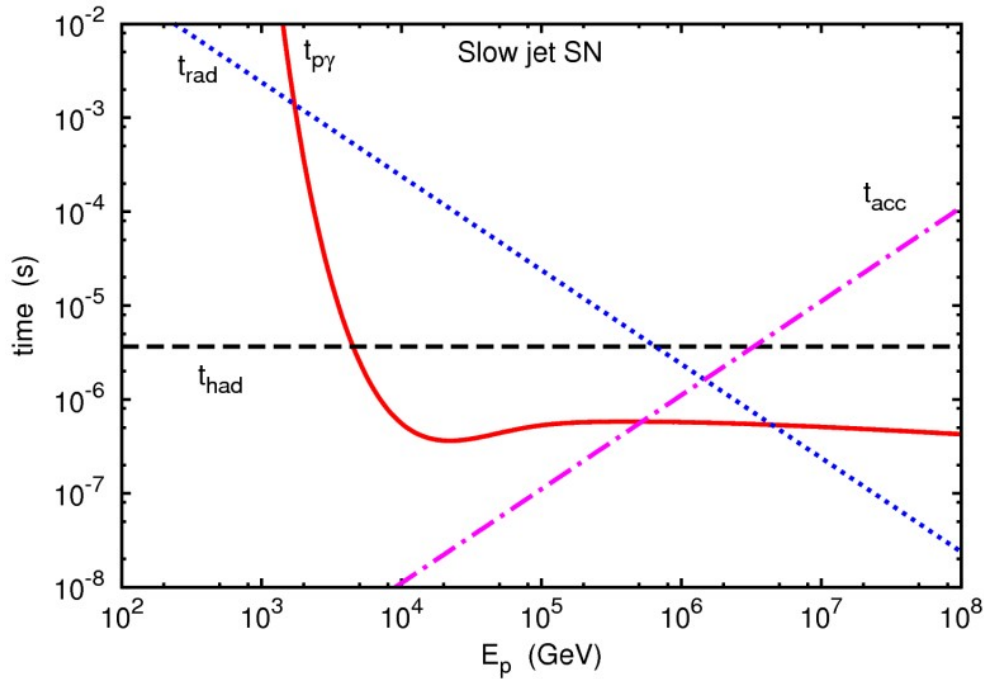
- Synchrotron and Inverse Compton scattering are the two EM (radiative) cooling mechanisms:

$$t'_{\text{syn},p} = \frac{6\pi m_p^4 c^3}{\sigma_T m_e^2 E'_p B'^2} \quad t'_{\text{IC},p} = \frac{3m_p^4 c^3}{4\sigma_T m_e^2 E'_p U'_\gamma}$$

$$(t'_{\text{rad},p})^{-1} = (t'_{\text{syn},p})^{-1} + (t'_{\text{IC},p})^{-1}$$

- Meson cooling times obtained by using meson mass
- Decay time scale is just $t'_{\text{dec},M} = (E'_M / m_M c^2) \tau_M$
- Note that non-rel Thompson cross section is used for IC: this is OK because IC is irrelevant for higher energies when cooling time becomes very large

Time scales for protons



[RE, M.H. Reno, I. Sarcevic, arXiv:0808.2807]

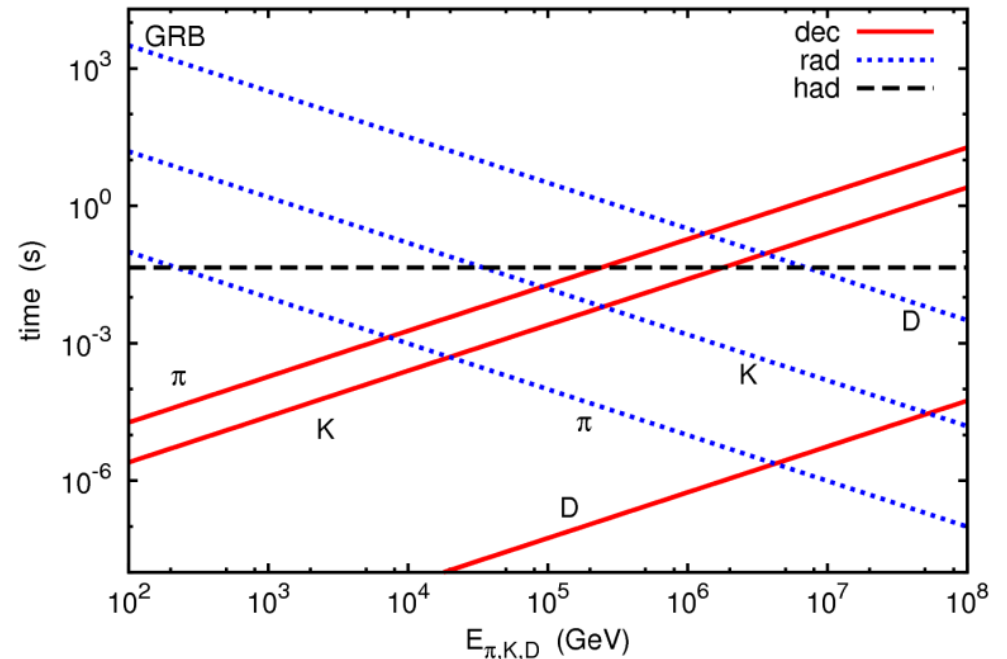
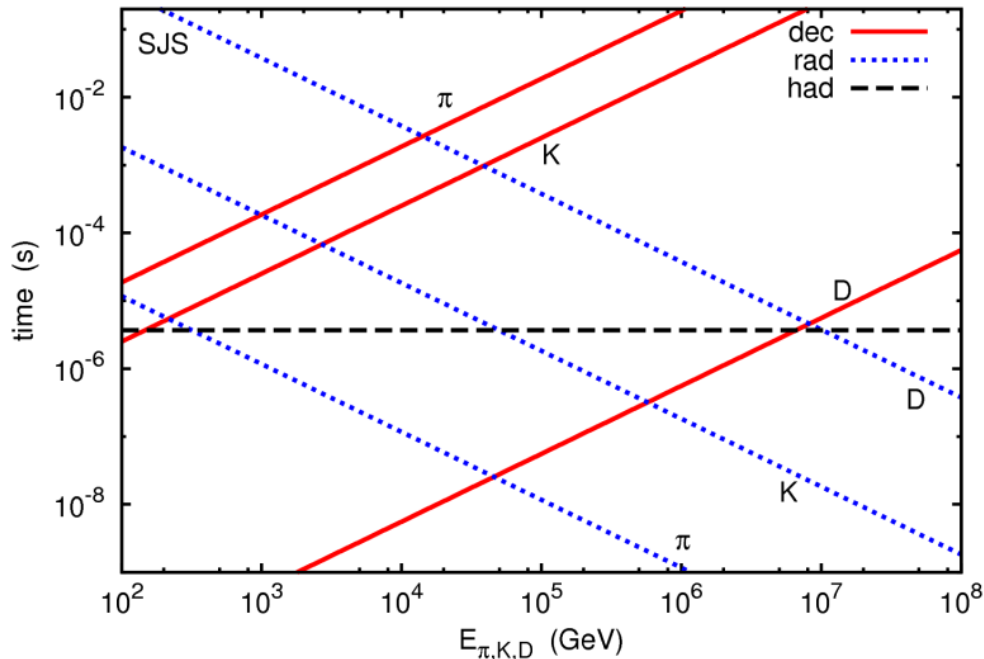
Maximum proton energy roughly estimated from when cooling times meet acceleration time

Above E_{max} there will be a rather quick drop-off in proton flux

Neutrino production

- $p\gamma$: charged pion decays from $p\gamma \rightarrow \Delta^+ \rightarrow n\pi^+$
and $\pi^+ \rightarrow \mu^+ \nu_\mu \rightarrow e^+ \nu_e \bar{\nu}_\mu \nu_\mu$
- pp : pions, kaons, D-mesons
- Proton spectrum is $\propto (E'_p)^{-2}$
- If no cooling, meson spectrum follows proton spectrum

Time scales for mesons



When cooling time gets shorter than decay time the meson flux becomes suppressed

- D-mesons decay before cooling until $E_D \sim 10^7$ GeV (SJS) or $E_D \sim 10^9$ GeV (GRB)
- Pions, kaons are cooled much earlier

Computation of neutrino flux

- We generalize the method of Z-moments to apply to sources
- Start with cascade equations for all species of particle j , schematically

$$\frac{d\phi_j}{dx} = -\frac{\phi_j}{\ell_j^{\text{tot}}} + S^{\text{tot}}(j p \rightarrow j Y)$$

- Use actual lengths x and l instead and assume constant density

Z-moments

- We calculate the Z-moments for charm production in the same way as for atmospheric charm
- For $pp \rightarrow \pi$ we use the parametrization (Costa et al)

$$\frac{dn_{\pi}}{dx_E} = 0.12 \frac{(1 - x_E)^{2.6}}{x_E^2}$$

and for $p\gamma \rightarrow \pi$ we fit this form to HERA data. For kaons we rescale pions by 0.1.

The flux

The neutrino flux is proportional to the proton flux:

$$\phi_{\nu}(E') = Z_{M\nu} \frac{L_M^{\text{eff}}}{L_M^{\text{dec}}} \frac{Z_{NM} \ell_N^{\gamma} + Z_{NM}^{\gamma} \ell_N^{\text{had}}}{\ell_N^{\text{had}} + \ell_N^{\gamma}} \phi_N(E')$$

This is the flux in the frame comoving with the jet.

We are interested in the flux in the Earth frame.

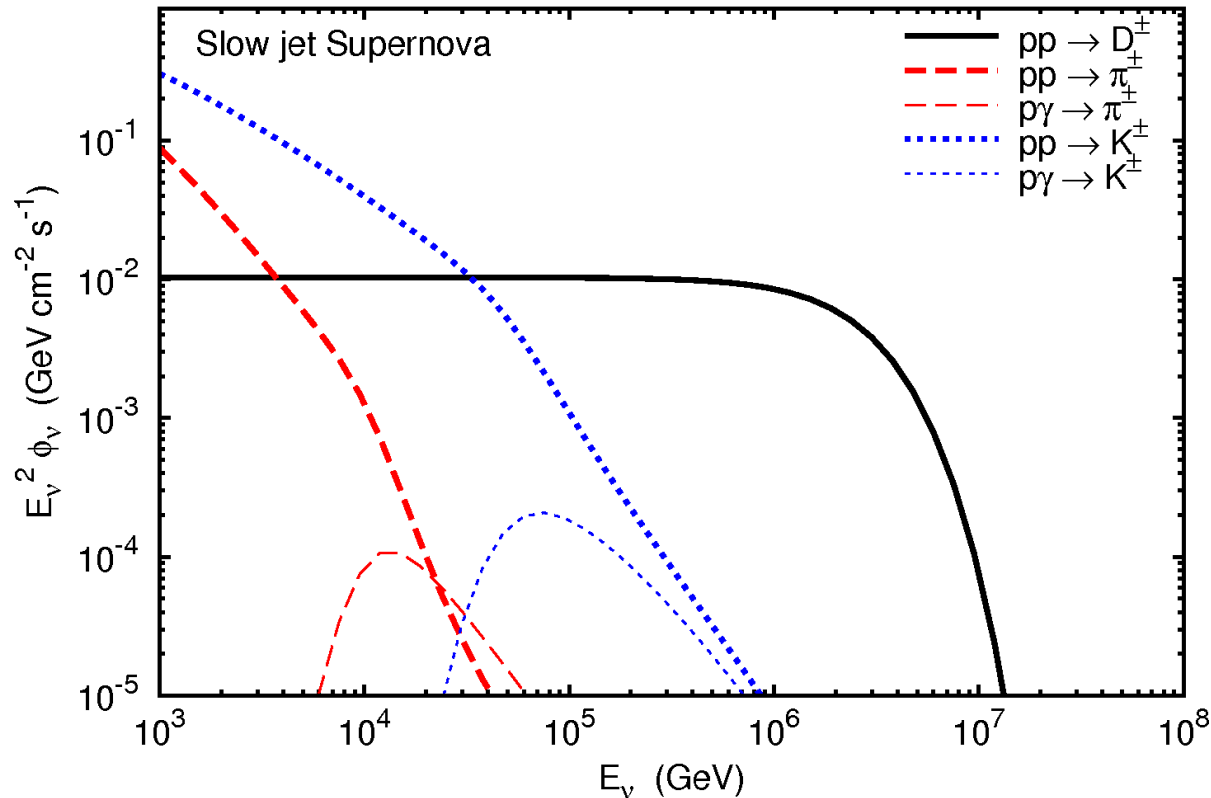
Normalization

The normalization of the flux from a single source depends on the overall luminosity, jet opening angle, jet Lorentz factor, and the distance:

$$\begin{aligned}\Phi_{\nu}(E) &= Z_{M\nu} \frac{L_M^{\text{eff}}}{L_M^{\text{dec}} (\ell_N^{\text{had}} + \ell_N^{\gamma})} \\ &\times (Z_{NM} \ell_N^{\gamma} + Z_{NM}^{\gamma} \ell_N^{\text{had}}) \\ &\times \frac{L_j \Gamma_j^2}{2\pi \theta_j^2 d_L^2 \ln(E'_{\text{max}}/E'_{\text{min}})} E^{-2}\end{aligned}$$

We choose $d_L = 20 \text{ Mpc} = 6 \times 10^{25} \text{ cm}$ (Virgo cluster)

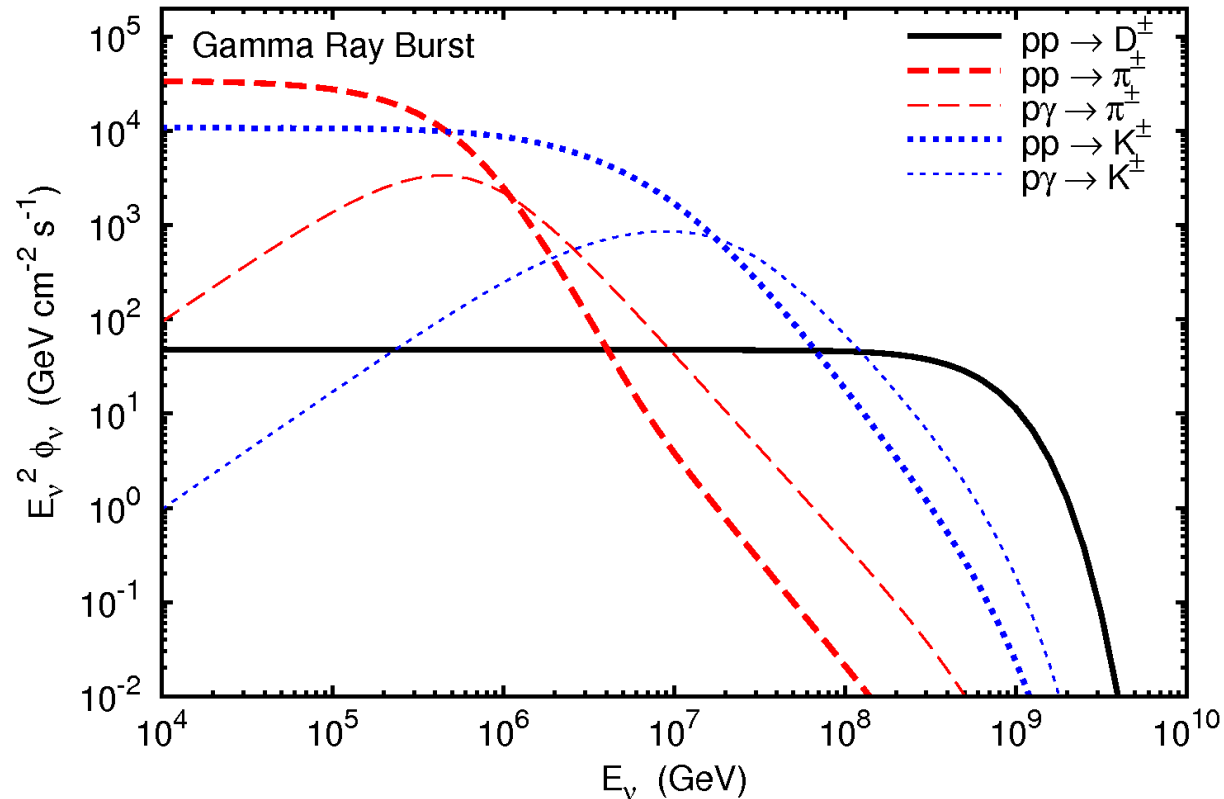
Neutrino flux from slow-jet SNe



[RE, M.H. Reno, I. Sarcevic, arXiv:0808.2807]

- No cooling of D-mesons
- Fall-off is due to maximum proton energy
(we use parameterization of Protheroe & Stanev, astro-ph/9808129)

Neutrino flux from GRB



- Again no cooling of D-mesons
- For this particular choice of parameters, charm has a smaller range where it dominates
- Some scenarios have much higher max proton energy

To be done

- We have done a toy-model calculation to show feasibility
- Look at detection prospects:
Both diffuse flux and single source
 - IceCube are already looking for single GRBs
(See also Gandhi, Samanta & Watanabe, in preparation)
- GRB parameters can vary widely
- More careful look at proton acceleration, cooling, source environment etc

Flavor ratios

- Pions lead to a 1:2:0 neutrino flavor ratio
- This is modified by oscillations to $\sim 1:1:1$
- D-mesons give an equal amount of ν_e and ν_μ
- Flavor ratios may be different at very high energy where charm dominates

Conclusions

- Atmospheric neutrinos are more or less guaranteed
- Astrophysical sources driven by jets are potential sources of high energy neutrinos
- Neutrinos can provide information on the nature of the source
- At low energies, primarily pions.
At intermediate energies, kaons dominate.
At very high energies, D-mesons may give the dominant contribution.

Backups follow

Protons and electrons

- The (comoving) density of protons and electrons in the jet is given by

$$n'_e = n'_p = \frac{L_j}{2\pi\theta_j^2 r_j^2 \Gamma_j^2 m_p c^3}$$

where L_j is the total jet power, Γ_j is the Lorentz factor and

$$r_j = 2\Gamma_j^2 c t_v$$

is the radius where the shock occurs

Photons and magnetic field

- The photon energy and number densities are

$$U'_\gamma = \frac{\epsilon_e L_j}{2\pi \theta_j^2 r_j^2 \Gamma_j^2 c} \quad n'_\gamma = 2\zeta(3) (15^3 / \pi^{14})^{1/4} \left(\frac{U'_\gamma}{\hbar c} \right)^{3/4}$$

for thermal photons and $U'_\gamma = n'_\gamma E'_\gamma$ for non-thermal

- The magnetic field is

$$B' = \left[\frac{4\epsilon_B L_j}{\theta_j^2 r_j^2 \Gamma_j^2 c} \right]^{1/2}$$

Z-moments for sources

- Z-moments are again defined as

$$Z_{kj} = \int_E^\infty dE' \frac{\phi_k(E')}{\phi_k(E)} \frac{\lambda_k^{\text{had}}(E)}{\lambda_k^{\text{had}}(E)} \frac{dn(k \rightarrow j; E', E)}{dE}$$

- Assume Feynman scaling, energy-independent cooling length, and power-law flux $\phi_N \sim E^{-\alpha}$:

$$Z_{NM} = \int_0^1 dx_E x_E^{\alpha-1} \frac{dn_{N \rightarrow M}}{dx_E}$$

where $x_E \equiv E_M / E_N$