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# New angles on top quark decay to a charged Higgs

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*work done with D. Eriksson, G. Ingelman, J. Rathsmann*  
JHEP 0801:024,2008, [arXiv:0710.5906 \[hep-ph\]](https://arxiv.org/abs/0710.5906)





# Top quark spin correlations

- At hadron colliders, pair-produced top quarks come in two spin configurations

$$\text{Singlet: } t_{\uparrow}\bar{t}_{\downarrow} \quad S=0$$

$$\text{Triplet: } t_{\uparrow}\bar{t}_{\uparrow}, t_{\uparrow}\bar{t}_{\downarrow}, t_{\downarrow}\bar{t}_{\downarrow} \quad S=1$$

- Measuring the spin projection of one top, the spin of the other top can be (statistically) determined *if* the overall spin is known.

Different production mechanisms (qq, gg, qg) give rise to corresponding parton level correlations:

$$\hat{C}_{ij}(M_{t\bar{t}}^2) = \frac{\hat{\sigma}_{ij}(t_{\uparrow}\bar{t}_{\uparrow} + t_{\downarrow}\bar{t}_{\downarrow}) - \hat{\sigma}_{ij}(t_{\downarrow}\bar{t}_{\uparrow} + t_{\uparrow}\bar{t}_{\downarrow})}{\hat{\sigma}_{ij}(t_{\uparrow}\bar{t}_{\uparrow} + t_{\downarrow}\bar{t}_{\downarrow}) + \hat{\sigma}_{ij}(t_{\downarrow}\bar{t}_{\uparrow} + t_{\uparrow}\bar{t}_{\downarrow})}$$

=> Modern day EPR experiment



# Spin correlations cont'd

## 1. Select spin quantization axes

**Helicity basis** → Spin quantized along momentum directions of  $t(\bar{t})$  in  $t\bar{t}$  CM frame

## 2. Determine parton level correlation as fcn. of inv. mass:

$$\text{Threshold: } \hat{C}_{q\bar{q}}(4m_t^2) = -\frac{1}{3} \quad \hat{C}_{gg}(4m_t^2) = 1$$

$$\text{Relativistic limit: } \hat{C}_{ij}(M_{t\bar{t}}^2 \rightarrow \infty) \rightarrow -1$$

## 3. Fold with pdfs and integrate to determine total correlation:

NLO calculation [Bernreuter et al, Nucl.Phys. B690 (2004) 81-137]

$$m_t = 175$$

Tevatron (qq dominated):  $\mathcal{C} = -0.352$

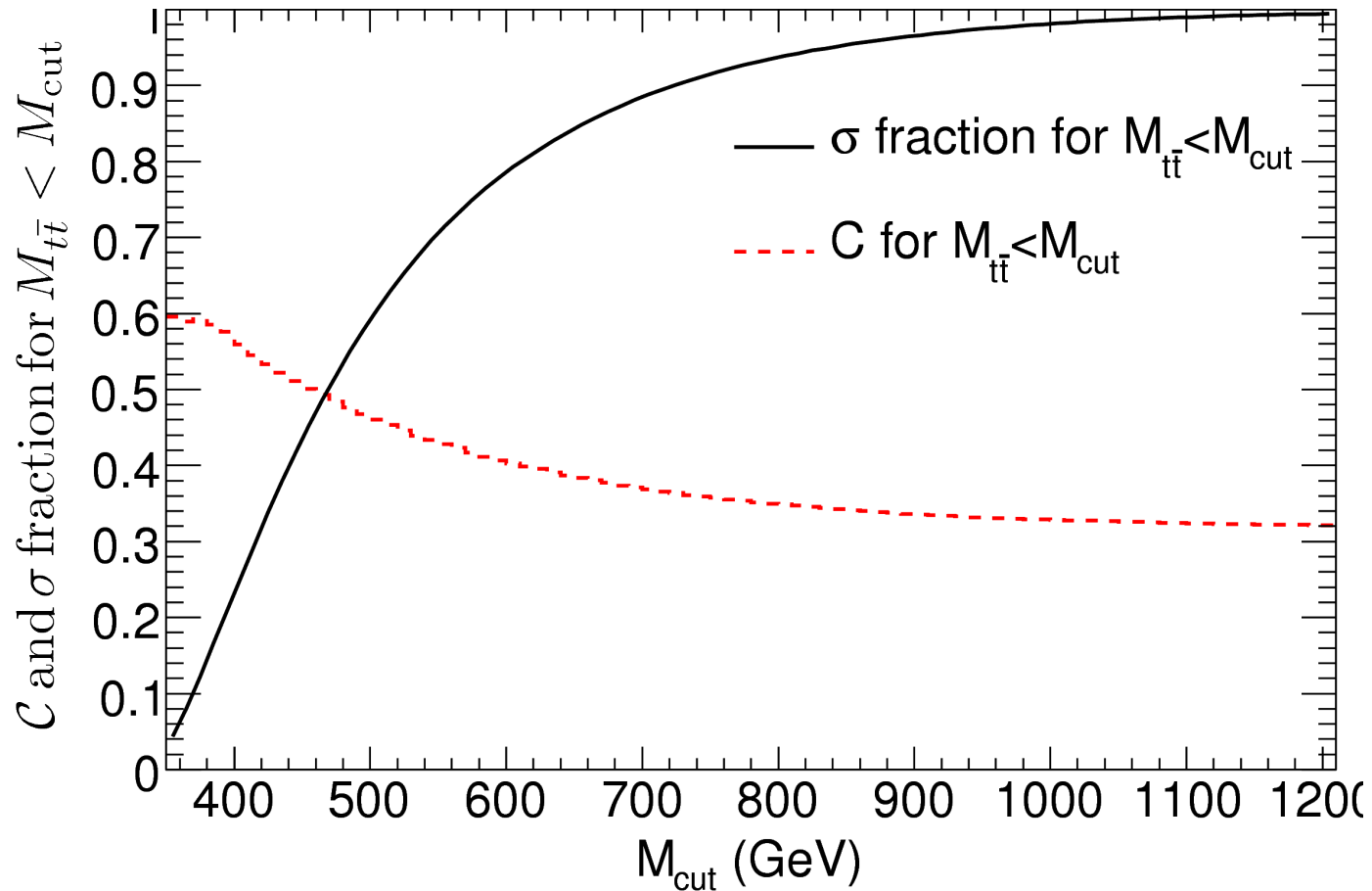
LHC (gg dominated):  $\mathcal{C} = 0.326$  (0.319 @ LO)

**Untested prediction of the Standard Model!**



# Increasing degree of correlation

- Applying an upper cut on invariant mass improves the degree of correlation at the LHC



- Remember high statistics at 14 TeV:  $\sigma(pp \rightarrow t\bar{t}) \simeq 900 \text{ pb}$



# Measuring the top quark spin

- Assume a fully polarized top in its rest frame with spin along z-axis. Weak decay encodes spin in distribution of decay products.

$$\frac{1}{\Gamma} \frac{d\Gamma}{d \cos \theta_i} = \frac{1 + \alpha_i \cos \theta_i}{2} \quad i = \{b, l^+, \nu_l, W^+\}$$

Spin analyzing coefficients  $\alpha_i$

$m_t = 175$

Best choice



Analyzing particle	$W^+$ ( $\omega = m_W^2/m_t^2$ )	Decay
$b$	$-\frac{1 - 2\omega}{1 + 2\omega}$	$\approx -0.4$
$W^+ / \mu^+$	$\frac{1 - 2\omega}{1 + 2\omega}$	$\approx 0.4$
$l^+ (\bar{d})$	1	1
$\nu_l (u)$	$\frac{(1 - \omega)(1 - 11\omega - 2\omega^2) - 12\omega^2 \ln \omega}{(1 - \omega)^2(1 + 2\omega)}$	$\approx -0.35$



# Measurement of spin correlations

- No net polarization of t quarks in helicity basis.
- Exploiting the correlation:

$$\frac{1}{N} \frac{d^2 N}{d \cos \theta_i d \cos \theta_j} = \frac{1}{4} \left( 1 + \mathcal{C} \alpha_i \alpha_j \cos \theta_i \cos \theta_j \right)$$

Doubly differential distribution with i,j from different tops.  
Angles determined in respective rest frames.

$$\mathcal{C}(\hat{\mathbf{a}}, \hat{\mathbf{b}}) = 4 \left\langle (\mathbf{S}_t \cdot \hat{\mathbf{a}})(\mathbf{S}_{\bar{t}} \cdot \hat{\mathbf{b}}) \right\rangle$$

- Alternatively use “opening angle”  $\cos \theta_{ij} = \hat{p}_i \cdot \hat{p}_j$   
and form the distribution

$$\frac{1}{N} \frac{dN}{d \cos \theta_{ij}} = \frac{1}{2} \left( 1 + \mathcal{D} \alpha_i \alpha_j \cos \theta_{ij} \right) \quad (-0.217 @ LO)$$

where  $\mathcal{D} = 4 \langle \mathbf{S}_t \cdot \mathbf{S}_{\bar{t}} \rangle = -0.24 @ NLO$  [Nucl.Phys. B690 (2004) 81-137]

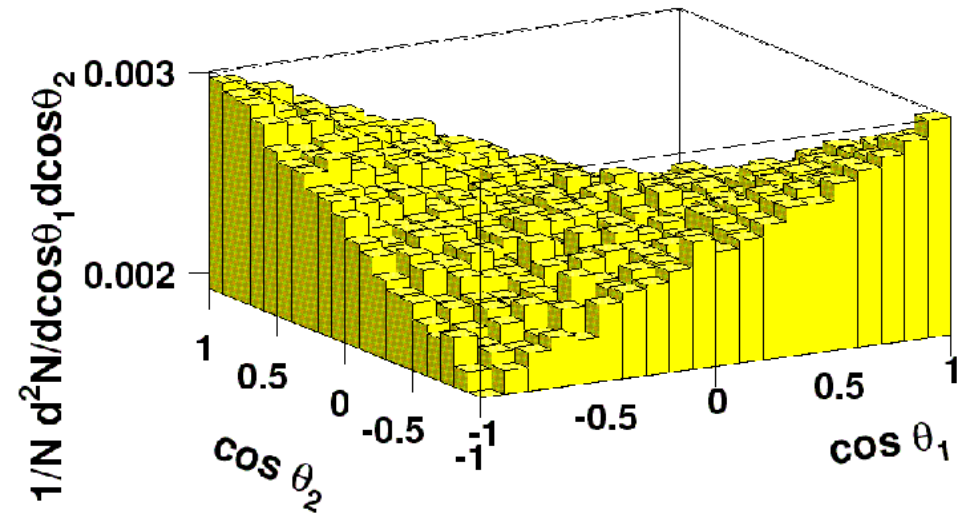
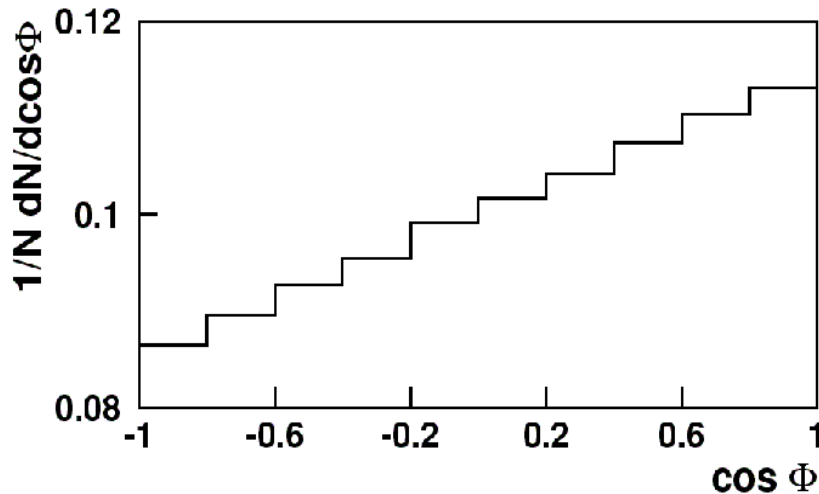
Less sensitive to acceptance loss by phase-space cuts



# Example: SM dilepton distributions

- Assuming top decay kinematics according to SM  
=> reconstruct tt rest frame in the dilepton channel.

$$pp \rightarrow t\bar{t} \rightarrow bW^+ \bar{b}W^- \rightarrow b\bar{b}l^+l^- \nu_l \bar{\nu}_l$$



- Experimentally: ATLAS study [F. Hubaut et al, hep-ex/0508061]

$$\Delta C/C \sim 6\% \quad \Delta D/D \sim 4\%$$

Systematics limited already with  $10 \text{ fb}^{-1}$

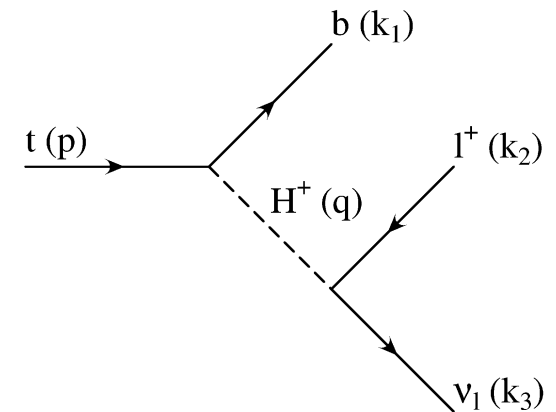
- High sensitivity → Possible to look for *new physics*



# Two-Higgs doublet models (2HDM)

- In the SM with one Higgs doublet, both charged dof. spent on  $W$  masses. => Only one neutral  $h$  left
- Adding another  $SU(2)_L$  Higgs doublet =>  $h, H, A, H^+, H^-$

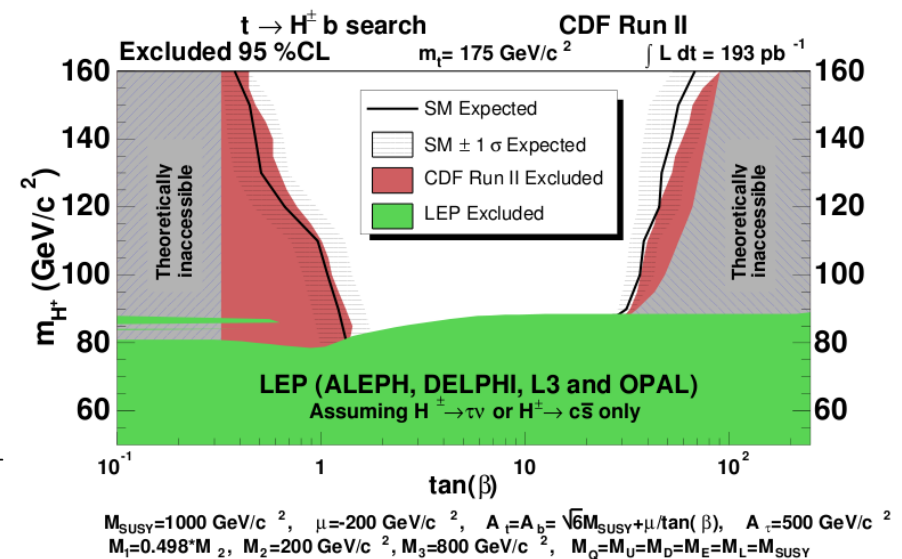
- Light  $H^+$  mediates top decay



- Absolute mass constraint from LEP:

$$m_{H^+} > m_W$$

- More stringent limits from Tevatron and B-fact. with some (a great deal of) model dependence
- Here we ignore the indirect constraints on  $m_{H^+}$





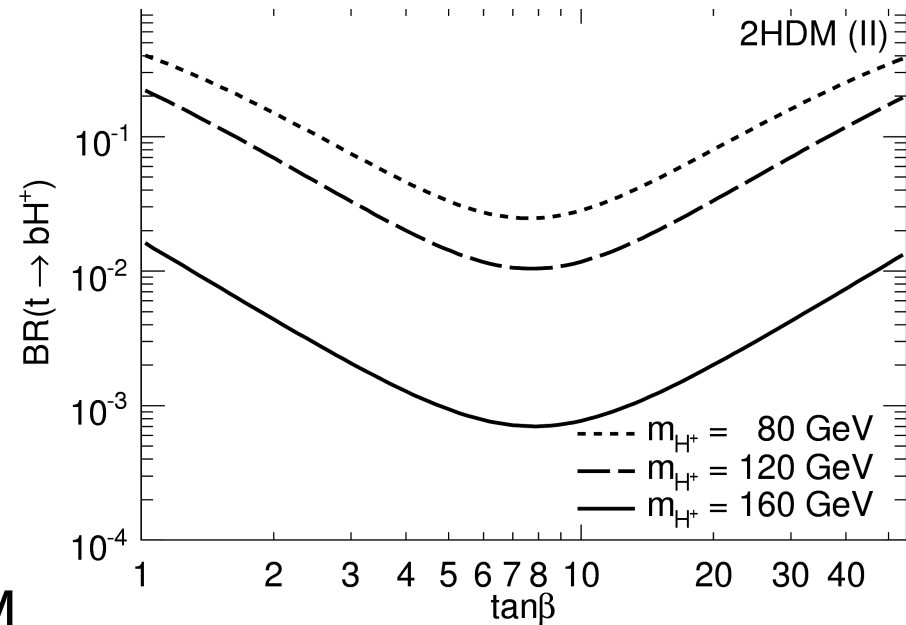
# Charged Higgs coupling structure

- Charged Higgs-fermion part of 2HDM Lagrangian:

$$\mathcal{L}_H = \frac{g_W}{2\sqrt{2}m_W} \sum_{\substack{\{u,c,t\} \\ \{d,s,b\}}} \left\{ V_{ud} H^+ \bar{u} \left[ A (1 - \gamma_5) + B (1 + \gamma_5) \right] d + \text{h.c.} \right\} \\ + \frac{g_W}{2\sqrt{2}m_W} \sum_{\{e,\mu,\tau\}} \left[ H^+ [C \bar{\nu}_l (1 + \gamma_5) l + H^- C^* \bar{l} (1 - \gamma_5) \nu_l] \right]$$

In MSSM

Coupling	2HDM (I)	2HDM (II)
$A$	$m_u \cot \beta$	$m_u \cot \beta$
$B$	$-m_d \cot \beta$	$m_d \tan \beta$
$C$	$m_l \cot \beta$	$m_l \tan \beta$



Real couplings in CP-conserving 2HDM

Large BR possible for large (small)  $\tan \beta$  values



# Spin analyzing coefficients for $t \rightarrow bH^+ \rightarrow b\tau^+ \nu_\tau$

- From decay density matrix we determine spin analyzing coefficients for the decay (after phase-space int.)

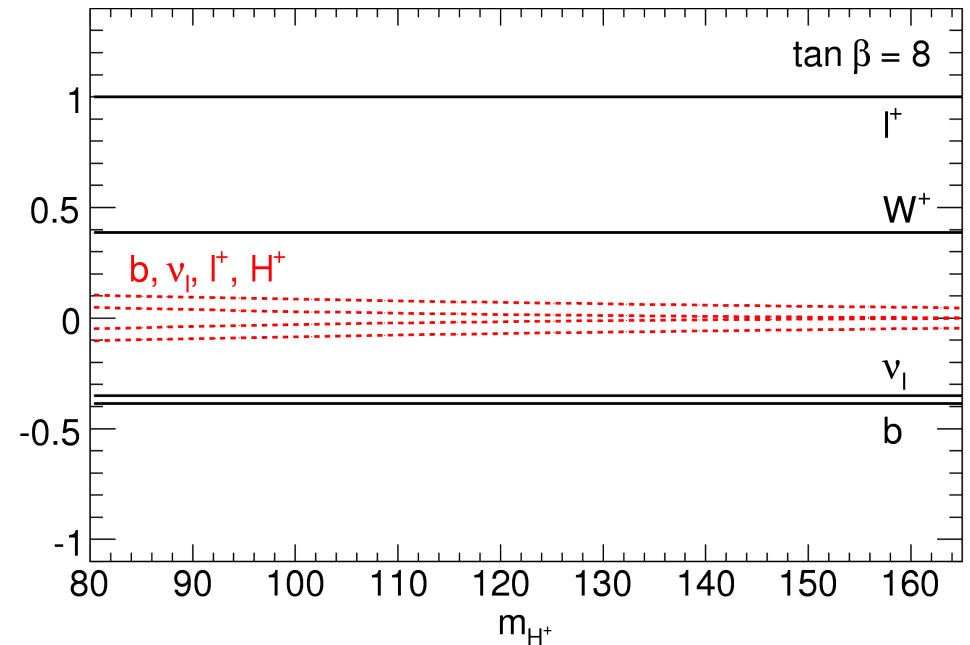
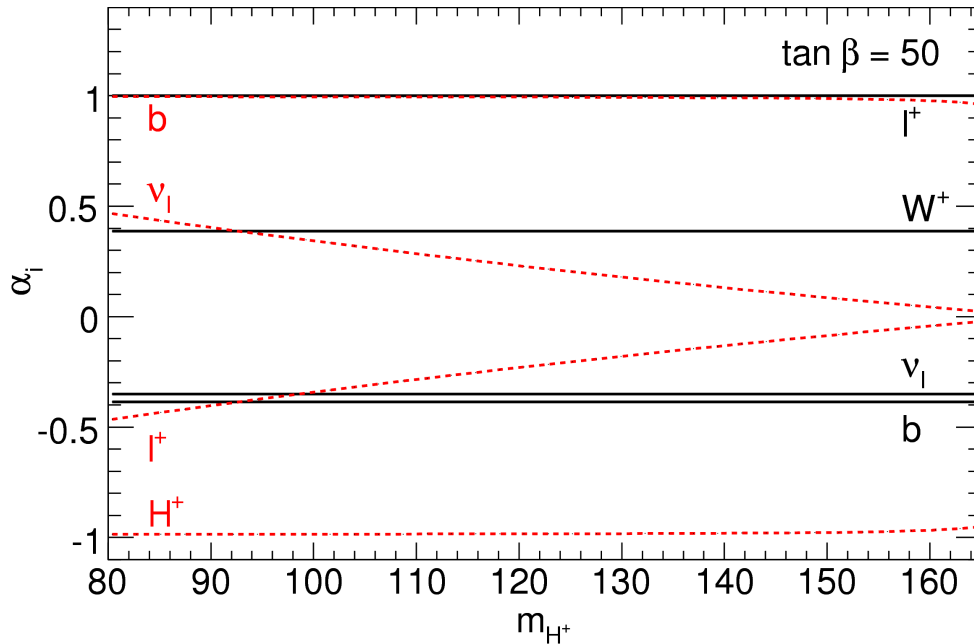
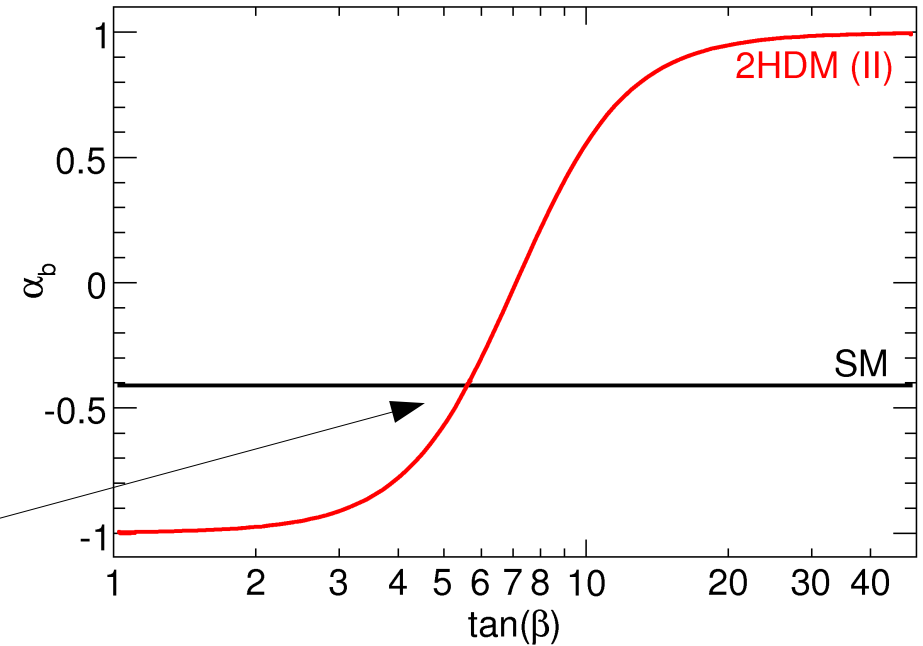
Analyzing particle	Decay channel	
	$W^+$ ( $\omega = m_W^2/m_t^2$ )	$H^+$ ( $\xi = m_{H^+}^2/m_t^2$ )
$b$	$-\frac{1-2\omega}{1+2\omega}$	$-\frac{A^2-B^2}{A^2+B^2} f(\xi, A, B)$
$W^+/H^+$	$\frac{1-2\omega}{1+2\omega}$	$\frac{A^2-B^2}{A^2+B^2} f(\xi, A, B)$
$l^+$ ( $\bar{d}$ )	1	$\frac{1-\xi^2+2\xi\ln\xi}{(1-\xi)^2} \frac{A^2-B^2}{A^2+B^2} f(\xi, A, B)$
$\nu_l$ ( $u$ )	$\frac{(1-\omega)(1-11\omega-2\omega^2)-12\omega^2\ln\omega}{(1-\omega)^2(1+2\omega)}$	$-\frac{1-\xi^2+2\xi\ln\xi}{(1-\xi)^2} \frac{A^2-B^2}{A^2+B^2} f(\xi, A, B)$

- Charged Higgs coefficients depends strongly on the universal coupling factor  $\frac{A^2-B^2}{A^2+B^2}$
- Threshold factor  $f(\xi, A, B) \simeq 1$  except for  $m_{H^+} \rightarrow m_t$



# Spin analyzing coefficients in 2HDM (II)

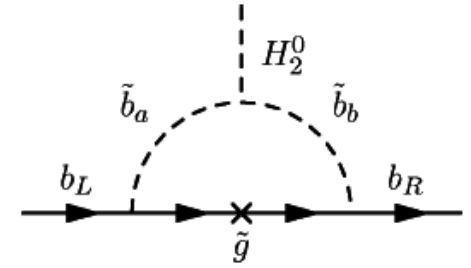
- Large differences from SM for high and low  $\tan \beta$
- Could give handle on charged Higgs coupling
- Fake SM at one point



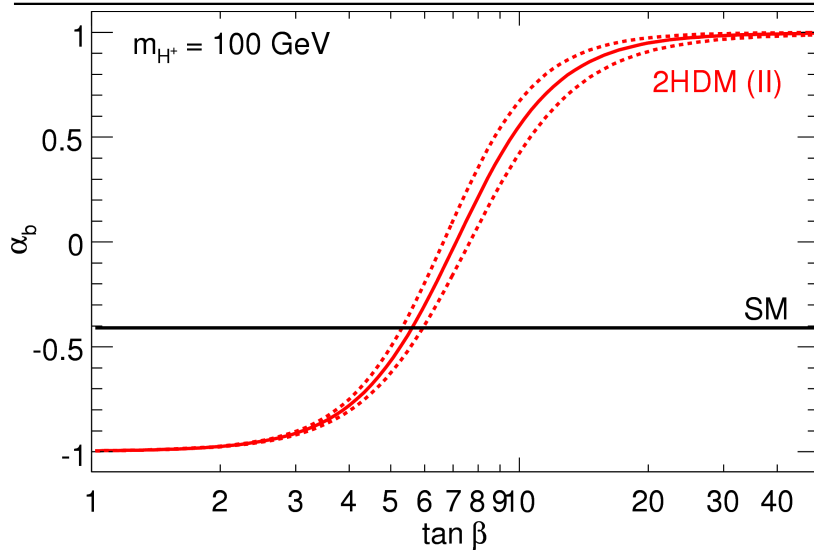


# Higher order corrections to SUSY 2HDM

- Yukawa coupling of quarks to “wrong” Higgs doublet induced at 1-loop level  
 $\tan \beta$  -enhanced corrections



Coupling	2HDM (I)	2HDM (II)	2HDM ( $\overline{\text{II}}$ )
$A$	$m_u \cot \beta$	$m_u \cot \beta$	$m_u \cot \beta [1 - \epsilon'_t \tan \beta]$
$B$	$-m_d \cot \beta$	$m_d \tan \beta$	$\frac{m_d \tan \beta}{1 + \epsilon_b \tan \beta}$
$C$	$m_l \cot \beta$	$m_l \tan \beta$	$m_l \tan \beta$



Decoupling limit:

$$\epsilon_b \sim \frac{\mu}{|\mu|} \frac{\alpha_s(M_{\text{SUSY}})}{3\pi} \simeq 10^{-2}$$

$$\epsilon_b = -\epsilon'_t = \pm 0.01$$

- Similar effect from standard NLO QCD corrections [hep-ph/0211098]

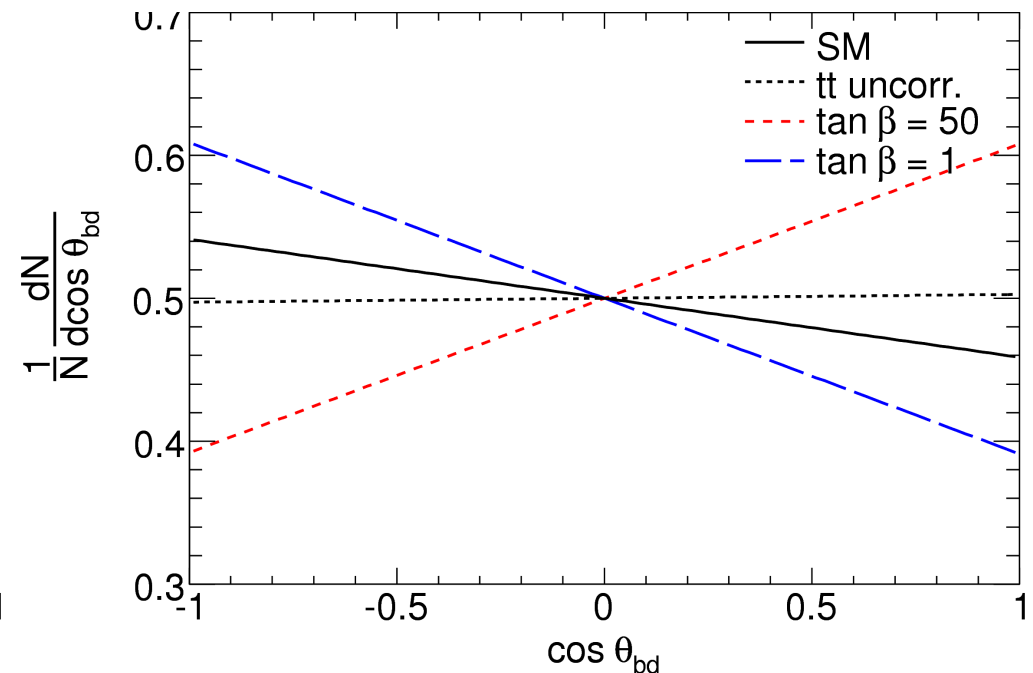
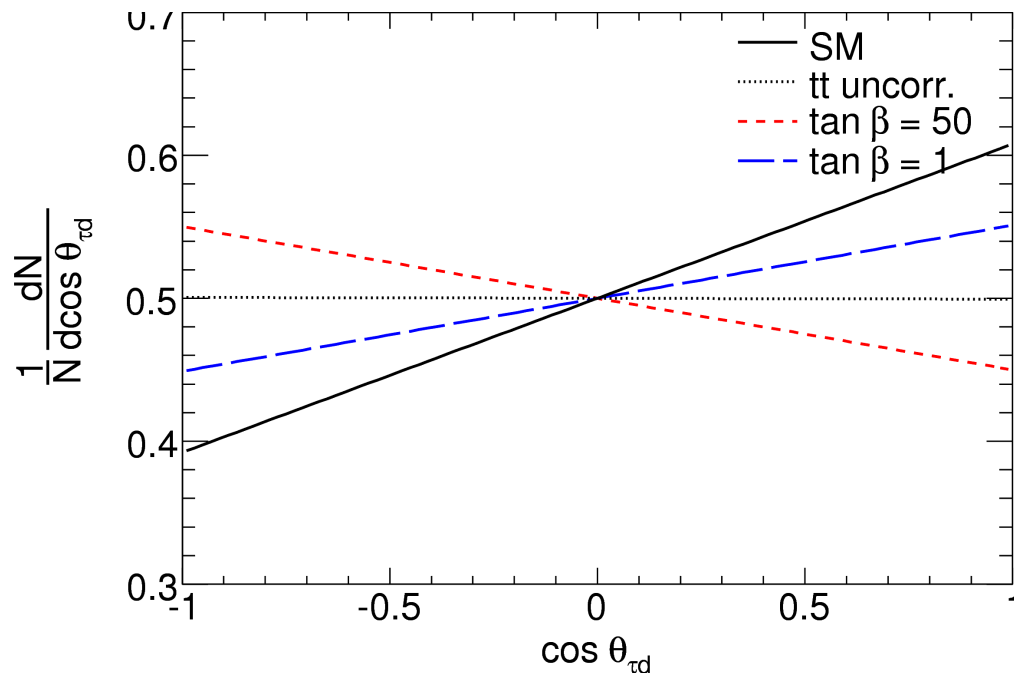


# Parton-level correlations in 2HDM (II)

- D-type distributions  $\frac{1}{N} \frac{dN}{d \cos \theta_{ij}} = \frac{1}{2} (1 + \mathcal{D} \alpha_i \alpha_j \cos \theta_{ij})$

$$t \rightarrow bH^+ \rightarrow b\tau^+ \nu_\tau$$

$$\bar{t} \rightarrow \bar{b}W^- \rightarrow \bar{b}\bar{u}d \quad + \text{cc.}$$



- Tau assumed stable here, full truth used to reconstruct CM

=> tau-d largest corr. in SM while b-d better for 2HDM



# From MC parton “truth” to hadron level

Problem: Charged Higgs decays to  $\tau$

- Almost no effect on e or  $\mu$  correlations
- Additional neutrinos from  $\tau$  decay  
=> Impossible to reconstruct partonic CM frame

Solution:

- Resort to hadronic decays of W and tau
- Reconstruct *transverse* rest frames of top quarks
- Measure azimuthal angles in these frames

In analogy with CM correlations we expect

$$\frac{1}{N} \frac{dN}{d \cos(\Delta\phi_i - \Delta\phi_j)} = \frac{1}{2} \left[ 1 + \mathcal{D}' \alpha_i \alpha_j \cos(\Delta\phi_i - \Delta\phi_j) \right]$$

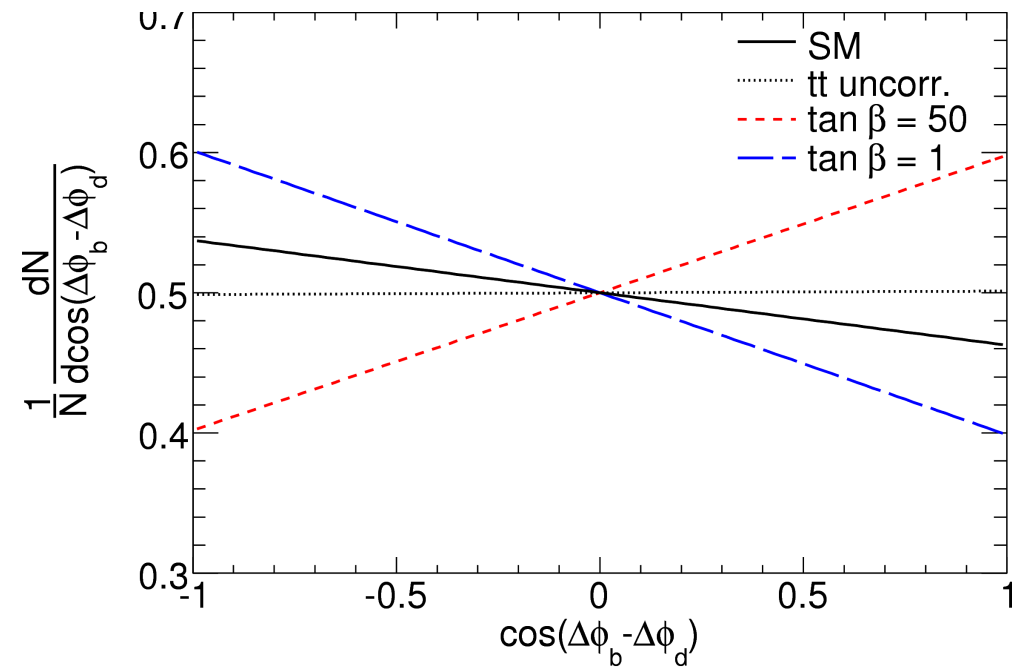
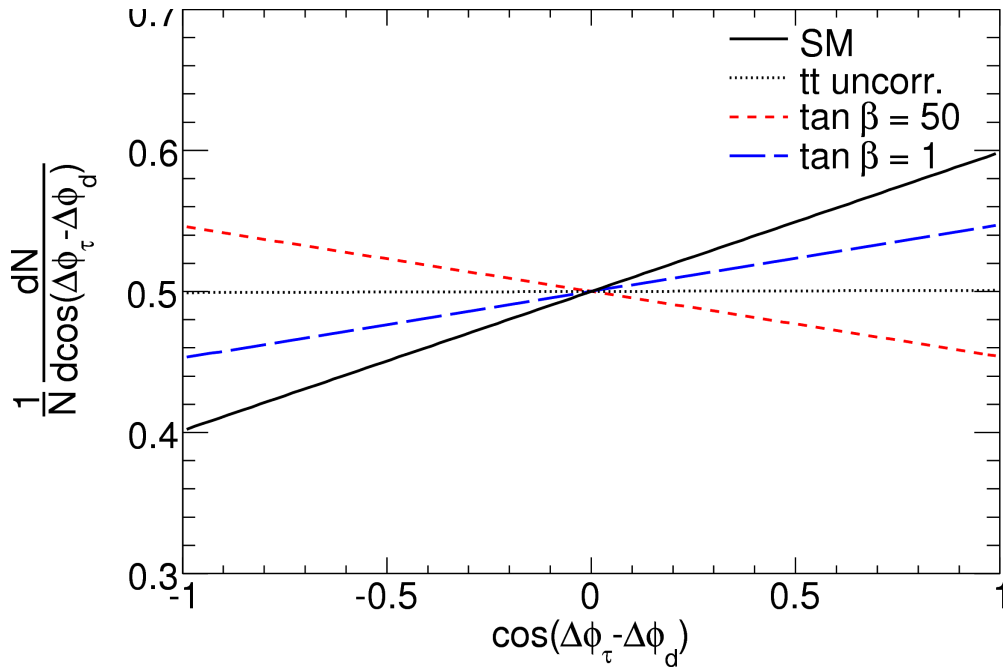
Numerically, we find for the LHC at LO:

$$\mathcal{D}' = 0.9\mathcal{D} \quad (\text{Remember that } \mathcal{D} = -0.217)$$



# Parton-level results from azimuthal angles

As before:  $t \rightarrow bH^+ \rightarrow b\tau^+\nu_\tau$   
 $\bar{t} \rightarrow \bar{b}W^- \rightarrow \bar{b}\bar{u}d$  + CC

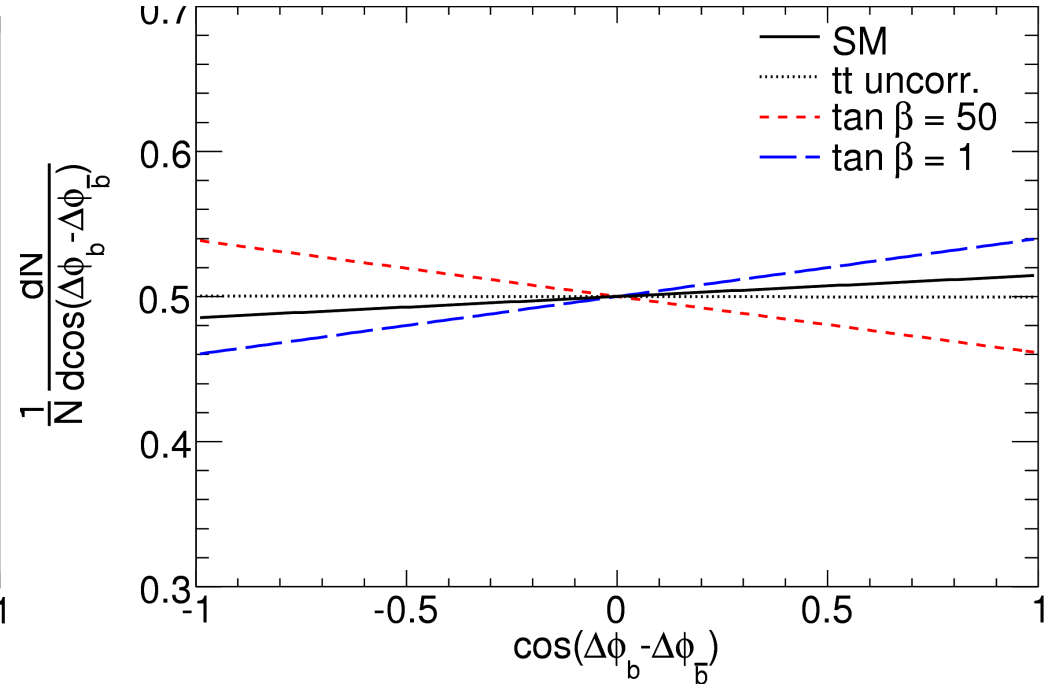
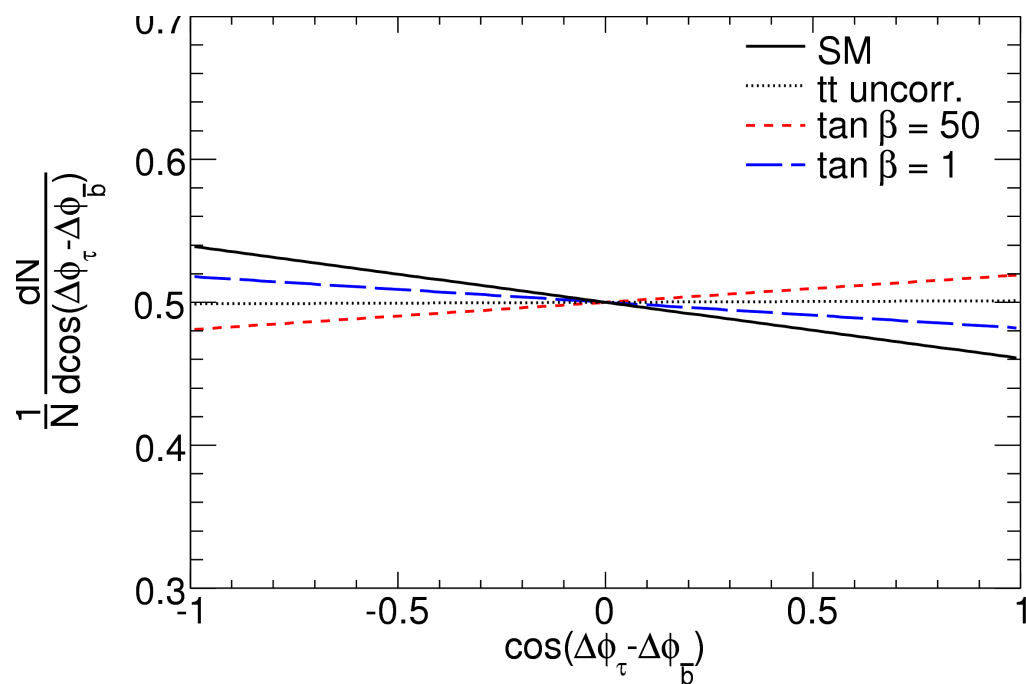


Encouraging results with this more useful observable



# Even more realism without light quark ID

- Low purity in identification of d-jets from W decay  
=>Use b quark identified with SM side  
(Another option is to use least energetic light jet)



- These distributions are what one could hope (in the best case) to test experimentally
- We started more modestly by checking the hadron level



# Hadron-level MC simulation

- Full  $2 \rightarrow 6$  ME from MadEvent, cross-check with TopReX  
Parton showering, hadronization, UE with PYTHIA

- Decay channels:  $t \rightarrow bH^+ \rightarrow b\tau^+ \nu_\tau$        $\tau \rightarrow$  hadrons  
with TAUOLA  
 $\bar{t} \rightarrow \bar{b}W^- \rightarrow \bar{b}\bar{u}d$

- Reconstruction:

$$|\eta| < 5$$

$$k_\perp \text{ jet finding } d_{\text{cut}} = 20 \text{ GeV}$$

“Flavor tagging”:  $\Delta R(\text{jet}, \text{parton}) < 0.4$      $|\eta| < 2.5$

W and top candidates from jet combinations

$$|m_{jj} - m_W| < 10 \text{ GeV}$$

$$|m_{jjb} - m_t| < 15 \text{ GeV}$$

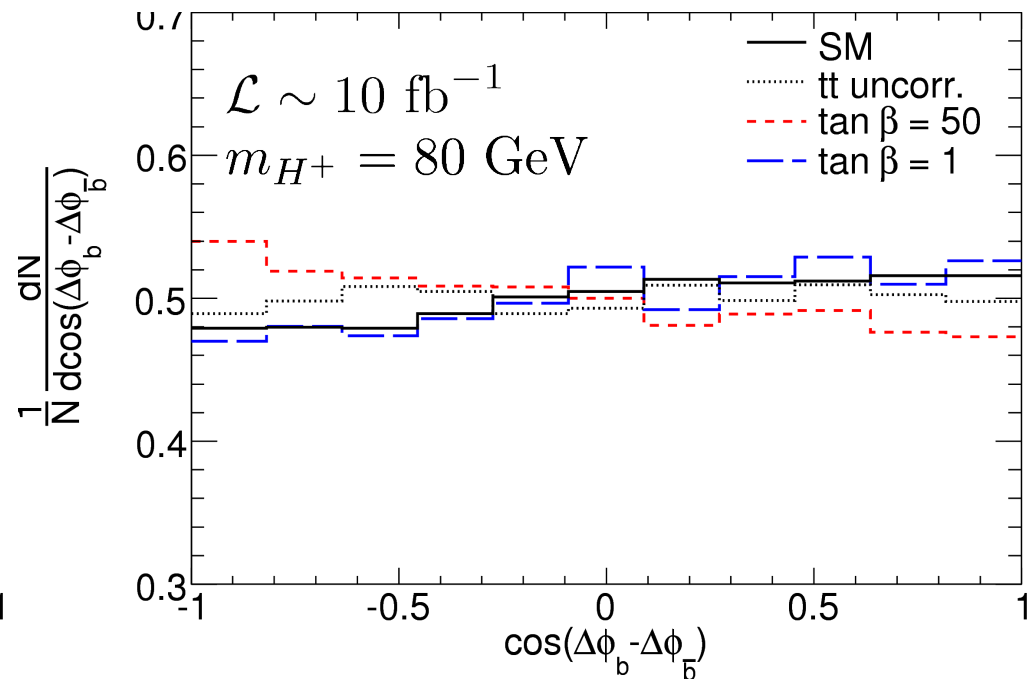
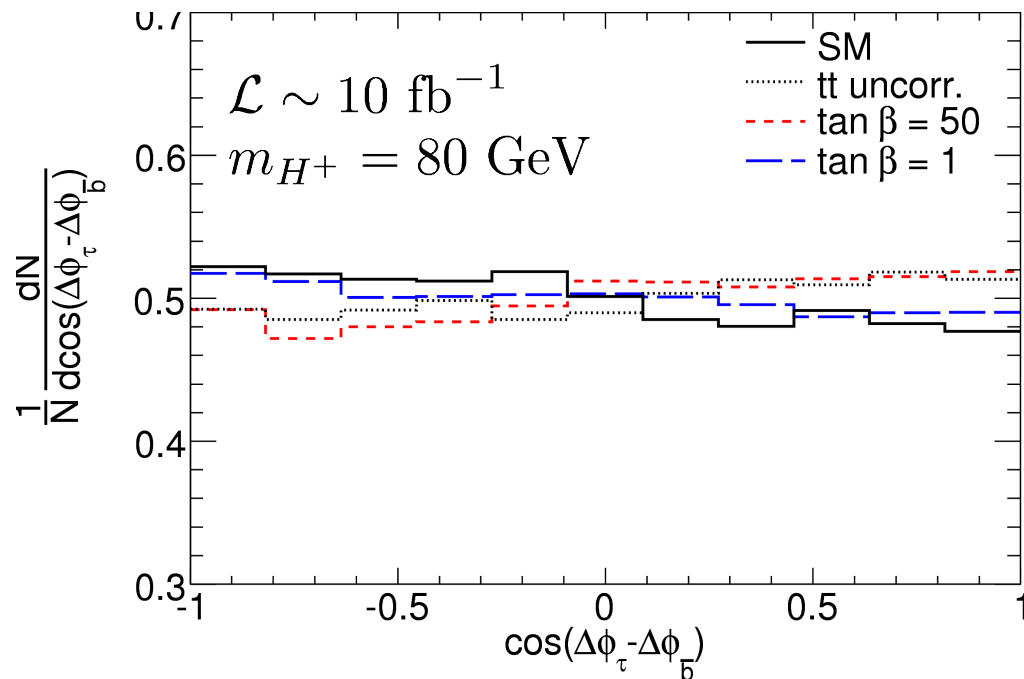
Analyzed events selected on basis of correct topology

- No backgrounds or detector effects at this point



# Hadron level - Final results

- From SM side of the event we use b quark as spin analyzer
- On  $H^+$  side we can use either tau jet or b jet



- Hadron level results similar to parton level (normalized dist)
- bb distribution most sensitive to new physics  
Hard enough b quark required  $\Rightarrow m_{H^+} \lesssim 130 \text{ GeV}$



# Summary and Conclusions

- Top quark spin correlations are predicted by the SM and should be tested at the LHC
- Large statistics expected for tt-events allows for new physics searches
- Charged Higgs bosons in top decays can influence angular distributions of top decay products in tau channel
- We have shown spin analyzing coefficients for 2HDM. SM lepton most efficient analyzer, b-quark (or  $H^+$ ) in 2HDM
- $H^+ \rightarrow \tau^+ \nu_\tau$  decay prevents reconstruction of rest frames. Partly solved by considering azimuthal distributions in transverse rest frames
- Hadron-level MC simulations show small  $H^+$  effect. Highest sensitivity for interesting case with large  $\tan \beta$