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# Quark Asymmetries in Nucleons

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J.A. and Gunnar Ingelman, [hep-ph/0503099](#)

[Phys. Rev. D 70, 111505 \(2004\)](#), [hep-ph/0407364](#)

[Phys. Lett. B 596, 77-83 \(2004\)](#), [hep-ph/0402248](#)



# Parton distributions in hadrons

- **Factorization theorems of QCD** separate soft and hard dynamics
- $Q^2$  dependence of parton distributions  $f_i(x, Q^2)$  given by the **DGLAP (Altarelli-Parisi) evolution** in perturbative QCD
- **Starting distributions**  $f_i(x, Q_0^2)$  **non-perturbative** and **non-calculable**
  - ↪ Usually parametrizations of arbitrary functions chosen to describe data
- **Valence** ( $u_v, d_v$ ), **gluon** and **sea** ( $q\bar{q}$ ) distributions
- Sea first believed to be symmetric ( $\bar{d} = \bar{u} = s = \bar{s}$ )
  - ↪ Soon  $s, \bar{s} \approx \frac{1}{2} \frac{\bar{d} + \bar{u}}{2}$  due to  $SU(3)$  violation
  - ↪ Also  $\bar{d} > \bar{u}$  (Gottfried sum rule violation)
- We have a **physically motivated model** for the starting distributions
  - ↪ **Insights into non-perturbative QCD dynamics**

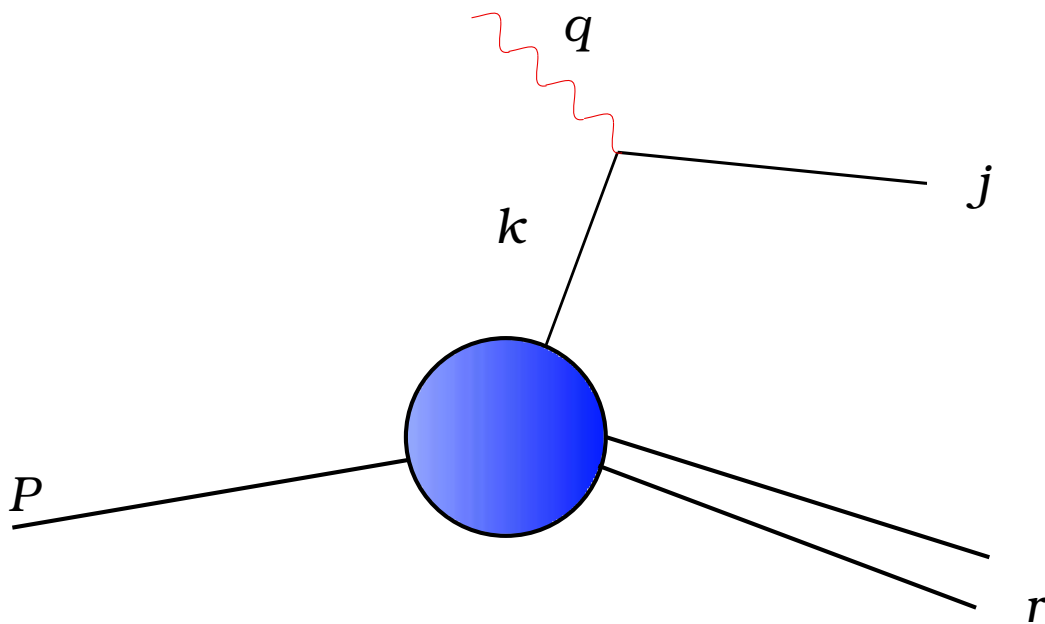


# Our Model: Valence distributions

In hadron rest frame:

- Parton momenta spherically symmetric
- Typical momentum from Heisenberg uncertainty:  $\langle k \rangle \sim \Delta p = \hbar/\Delta x \sim 200 \text{ MeV}$

Gaussian momentum fluctuations ( $k^\mu \in N(0, \sigma_i)$ ) of partons:



Use  $z$ -boost invariant  $x = \frac{k_+}{P_+} = \frac{E_k + k_z}{E_P + P_z}$

Kinematic constraints:

$$0 < j^2 < W^2 = (P + q)^2$$

$$r^2 > 0$$

$\Rightarrow 0 \leq x \leq 1$  and  $f_i(x) \rightarrow 0$  as  $x \rightarrow 1$

Monte Carlo-simulate to get  $x$  distribution.

# Analytical expressions

Integrating over  $k_{\perp}^2$  and  $k_{-}$ :

$$f_i(x) = N(\tilde{\sigma}_i, \tilde{x}_i) \left\{ \left[ 1 + \operatorname{erf} \left( \frac{1-\tilde{x}_i}{2\tilde{\sigma}_i} \right) \right] \exp \left[ -\frac{(x-\tilde{x}_i)^2}{4\tilde{\sigma}_i^2} \right] - \left[ 1 + \operatorname{erf} \left( \frac{x-\tilde{x}_i}{2\tilde{\sigma}_i} \right) \right] \exp \left[ -\frac{(1-\tilde{x}_i)^2}{4\tilde{\sigma}_i^2} \right] \right\}$$

where  $\tilde{\sigma}_i \equiv \sigma_i/M$ ,  $\tilde{x}_i \equiv m_i/M$

Approximately

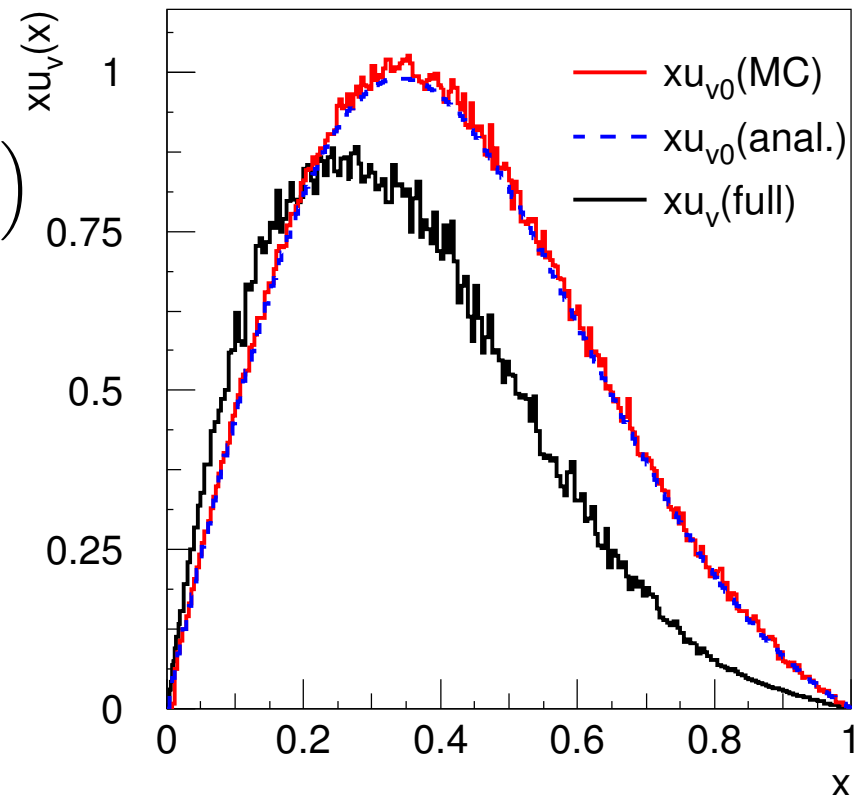
$$f_i(x) = N(\tilde{\sigma}_i, \tilde{x}_i) \left[ 1 - \exp \left( \frac{1-x}{2\tilde{\sigma}_i^2} \right) \right] \exp \left( -\frac{(x-\tilde{x}_i)^2}{4\tilde{\sigma}_i^2} \right)$$

Note: for  $x \gtrsim 0.9$   $f_i(x) \sim (1-x)^1$

**BUT** for  $0.3 \lesssim x \lesssim 0.9$ :

$xu(x) \sim x(1-x)^{2.8}$  (cf. counting rules)

$x \lesssim 0.7$ : Shape modified by **hadronic fluctuations**

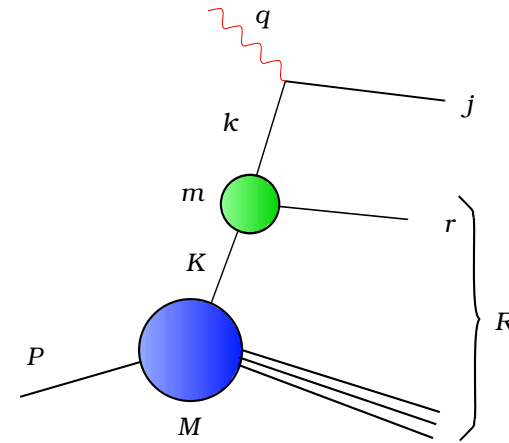


# Our Model: Sea distributions

- **Hadronic quantum fluctuations:**

$$|p\rangle = \alpha_0|p_0\rangle + \alpha_{p\pi^0}|p_0\pi^0\rangle + \alpha_{n\pi^+}|n\pi^+\rangle \\ + \dots + \alpha_{\Lambda K}|\Lambda K^+\rangle + \dots$$

- **Gaussian momentum distribution** of meson and baryon (in  $P$  rest frame)
- **Photon probes parton in meson or baryon**
- **Normalization: fit effective  $\alpha_{BM}^2$**  effectively including Clebsch-Gordan coefficients, unknown mass suppression and mixing of states



$$x_H = K_+ / (K + K_{\text{partner}})_+$$

$$x_p = k_+ / K_+$$

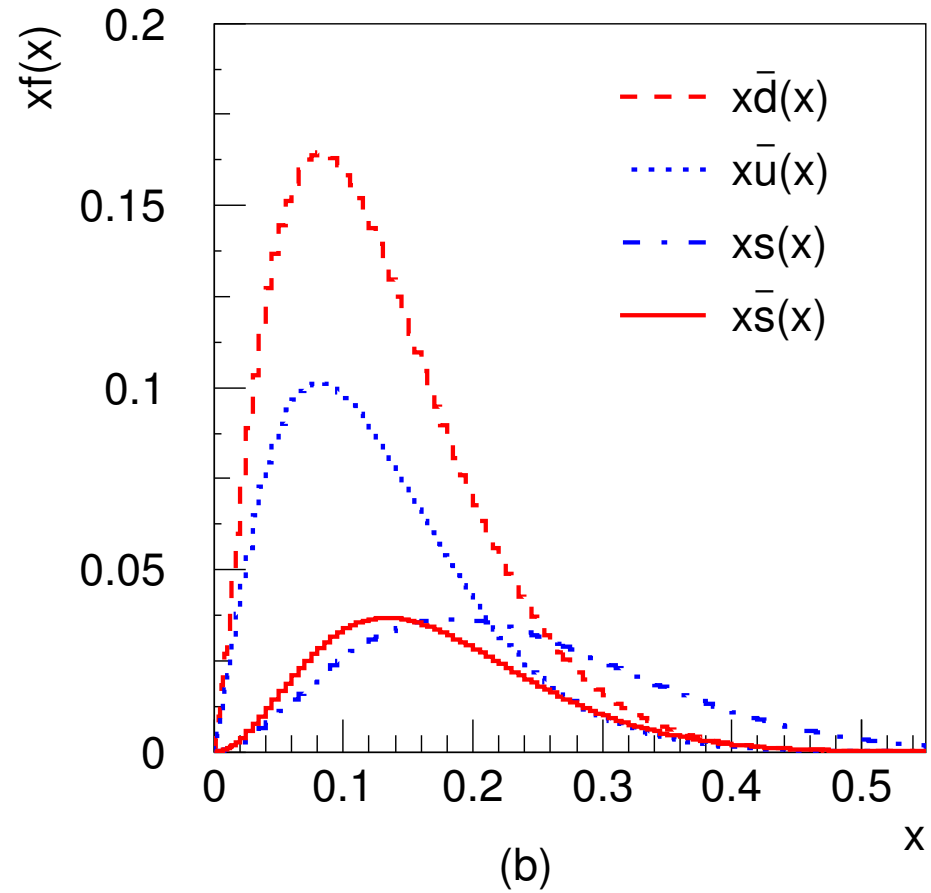
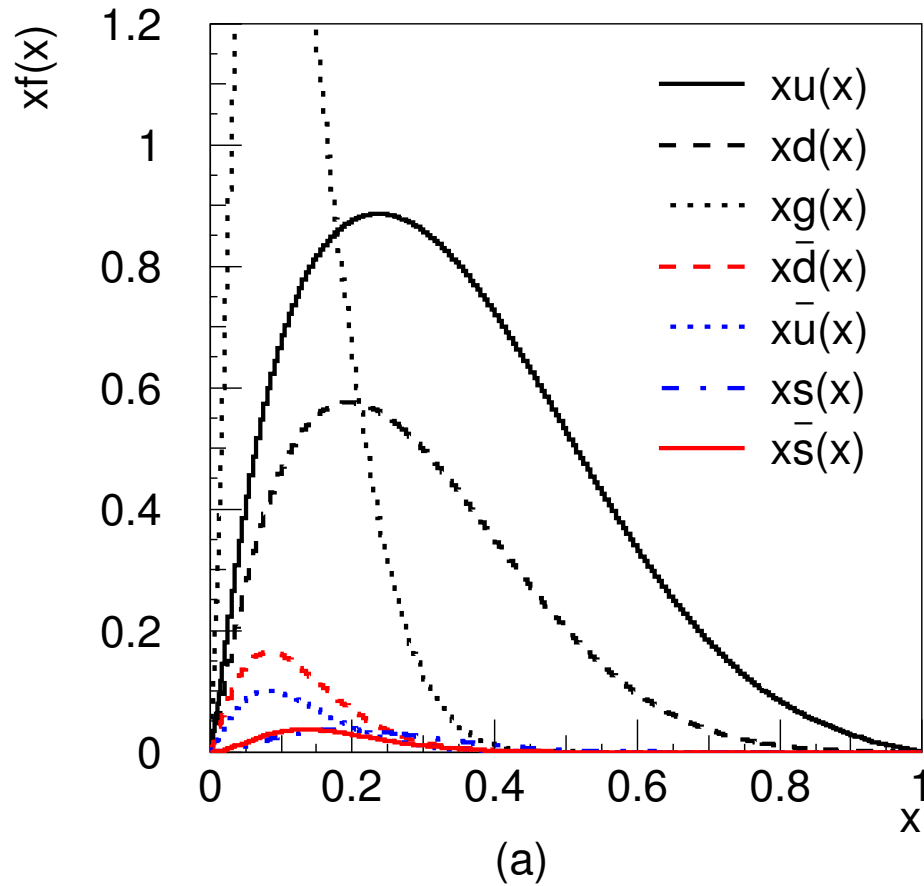
$$x = x_H \cdot x_p$$

Kinematic constraints:

$$0 < j^2 < W_H^2 = (K + q)^2$$

$$r^2 > 0, R^2 > 0$$

# Resulting distributions



Shapes agree well with parametrizations (as will be shown below)

# Parameters and experimental data

Parameters:

$$\begin{aligned}\sigma_u &= 230 \text{ MeV} & \sigma_d &= 170 \text{ MeV} & \sigma_g &= 77 \text{ MeV} & \sigma_H &= 100 \text{ MeV} \\ \alpha_{p\pi^0}^2 &= 0.45 & \alpha_{n\pi^+}^2 &= 0.14 & \alpha_{\Lambda K}^2 &= 0.05 \\ Q_0 &= 0.75 \text{ GeV}\end{aligned}$$

DGLAP evolution:

QCDNUM16: NLO evolution in  $\overline{MS}$  scheme

Experimental data sets (to fix the free parameters):

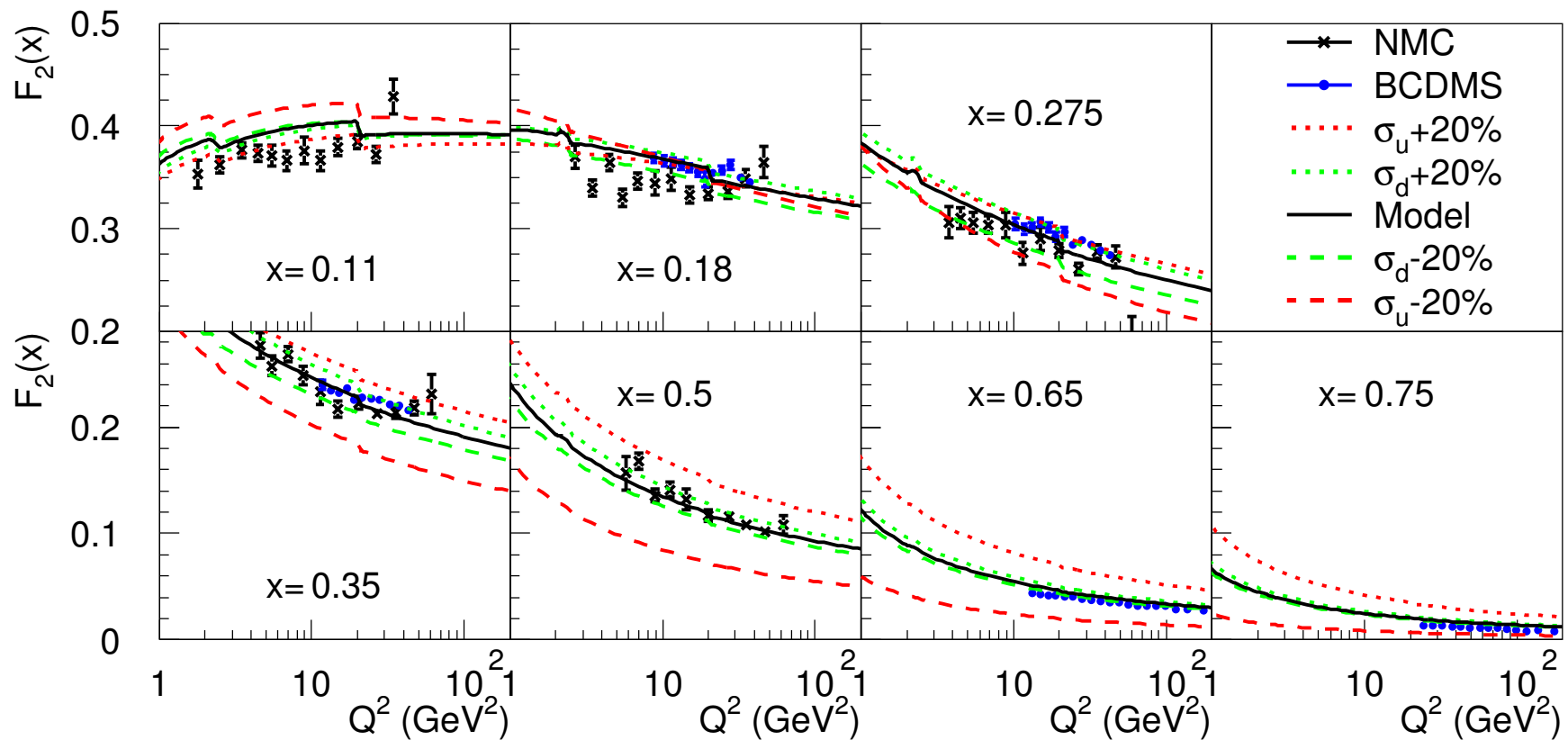
- Fixed-target  $F_2$  data
- HERA  $F_2$  data
- $W^\pm$  charge asymmetry data
- $\bar{d}/\bar{u}$ -asymmetry data
- Strange sea data

Simultaneous fit to all data sets



# Fixed-target DIS data

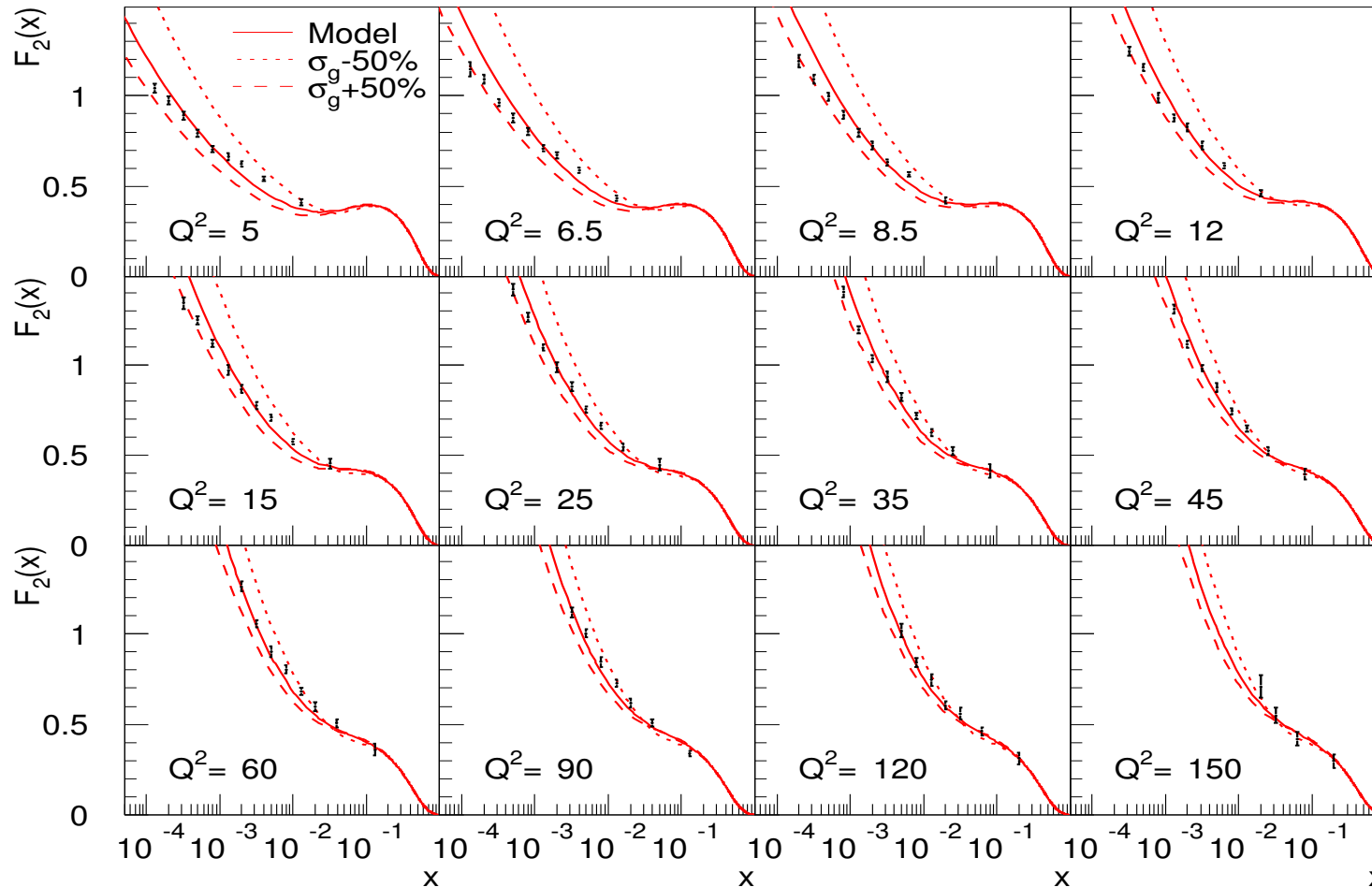
NMC and BCDMS  $F_2$  data fixes large- $x$  valence distributions ( $\sigma_u, \sigma_d$ )



Harder constraints on  $u$  distribution than on  $d$  distribution

# HERA DIS data

H1 small- $x$   $F_2$  data fixes gluon distribution ( $\sigma_g$ ) and starting scale  $Q_0$



# $W^\pm$ asymmetry data

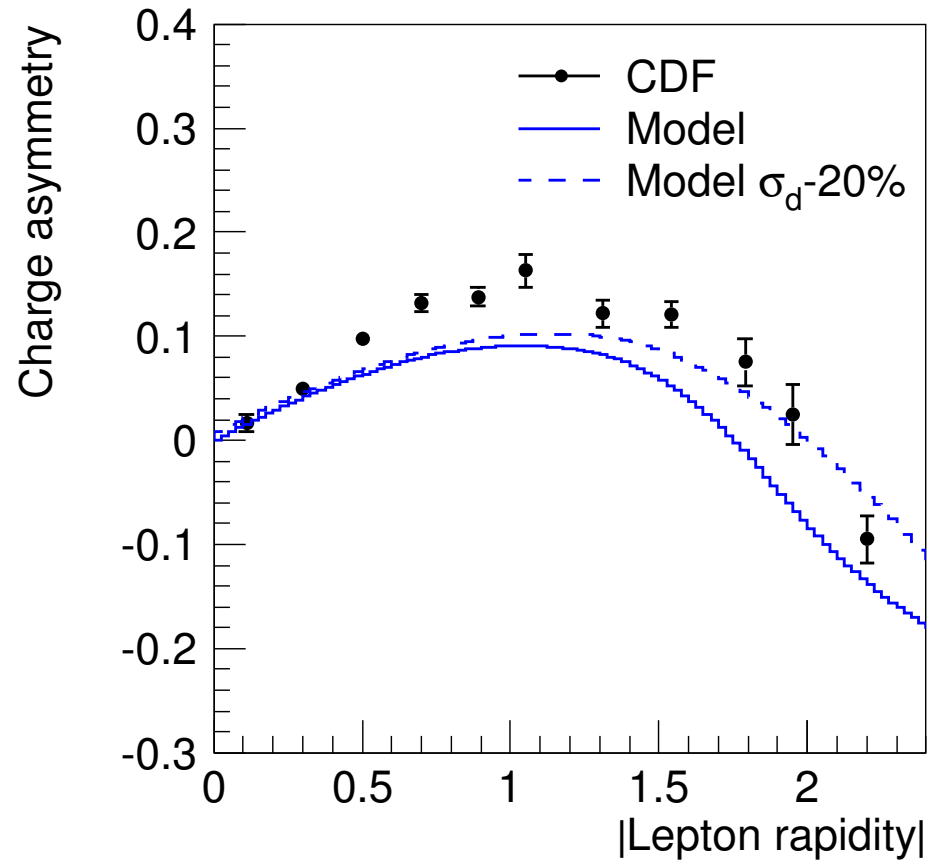
In  $p\bar{p}$ -collisions at Tevatron:

$$\left. \begin{array}{l} u\bar{d} \rightarrow W^+ \rightarrow l^+\nu_l \\ d\bar{u} \rightarrow W^- \rightarrow l^-\bar{\nu}_l \end{array} \right\} \Rightarrow$$

charged lepton forward-backward asymmetry if different  $u$  and  $d$  spectrum:

$$A(y_l) = \frac{d\sigma^+/dy_l - d\sigma^-/dy_l}{d\sigma^+/dy_l + d\sigma^-/dy_l}$$

In our model: Different Gaussian widths  $\sigma_u$  and  $\sigma_d$  (due to Pauli exclusion?)

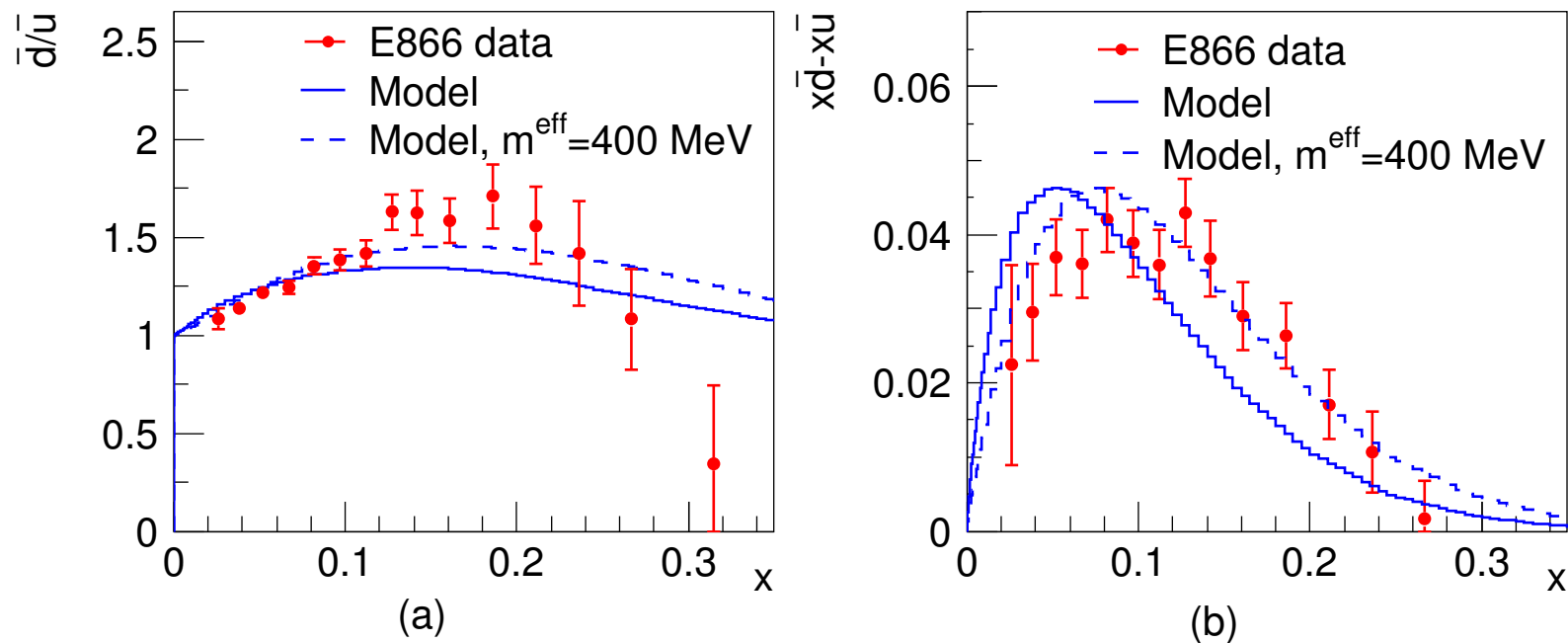


# The $\bar{d} - \bar{u}$ asymmetry

Pert. QCD  $g \rightarrow q\bar{q}$  gives  $\bar{d} - \bar{u}$  symmetry, but no symmetry forbids  $d\bar{d} \neq u\bar{u}$

Fluctuations  $p \rightarrow p\pi^0$ ,  $p \rightarrow n\pi^+$ , but only  $p \rightarrow \Delta^{++}\pi^- \Rightarrow$  excess of  $\bar{d}$  over  $\bar{u}$

Fitted parameters to Drell-Yan data in  $pp$  and  $pd$  scattering:  $\alpha_{p\pi^0}^2$  and  $\alpha_{n\pi^+}^2$



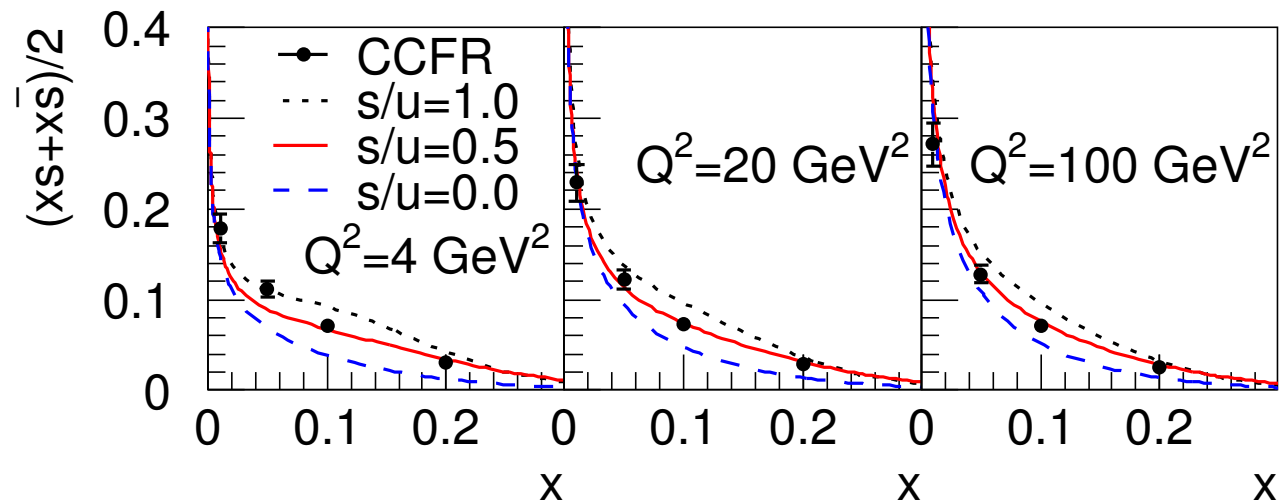
Note: Position of peak better described with effective pion mass  $m^{\text{eff}} \approx 400$  MeV may account for heavier mesons, *e.g.*  $|N\rho\rangle$ , or generic meson states?

## The strange sea

Lightest strange fluctuation  $p \rightarrow \Lambda K^+$

Heavier fluctuations ( $|\Sigma K\rangle, |\Lambda K^*\rangle$ ) effectively included by fit

Normalization  $\alpha_{\Lambda K}^2$  given by comparison to CCFR  $\nu_\mu N \rightarrow \mu + c + X$  data



$(s + \bar{s})/(\bar{u} + \bar{d}) \approx 0.5$  as

- pdf parameterisations

- hadronisation models:

$$\text{Lund } \frac{P(s\bar{s})}{P(u\bar{u} + d\bar{d})/2} \simeq \frac{1}{3}$$

Norm  $\sim 1/\Delta M_{BM}$  (not  $1/\Delta E_{BM}^2$ , as in OFPT)

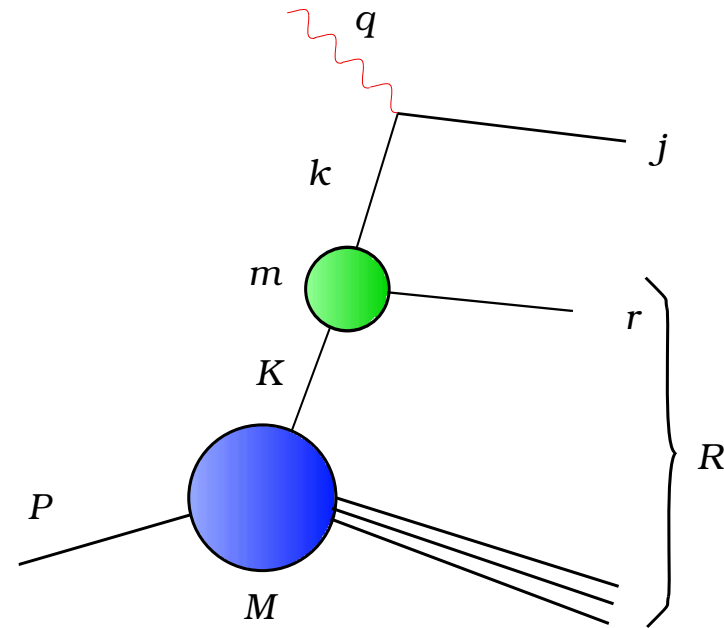
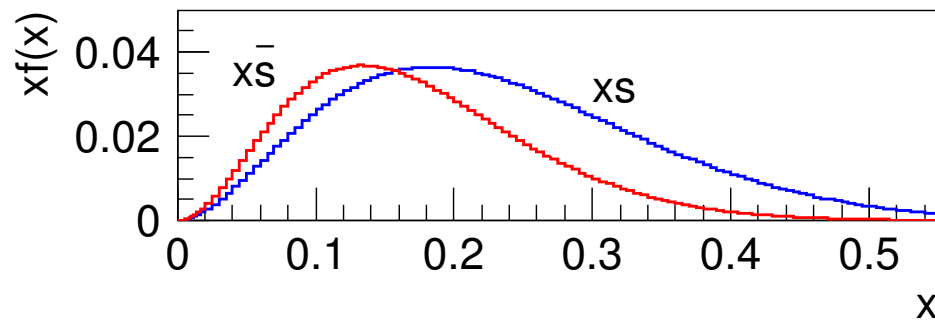
# Asymmetry of the strange sea

Remember:

$$x = x_H \cdot x_p$$

$$x_H = K_+ / (K + K_{\text{partner}})_+ \\ \approx M_H / (M_{\text{meson}} + M_{\text{baryon}})$$

- $s$  quark in (heavier) baryon  $\Lambda$
- $\bar{s}$  quark in (lighter) meson  $K^+$



$s$  distribution harder than  $\bar{s}$  distribution

*Cf.* Brodsky and Ma, Phys. Lett. B **381**, 317 (1996)

## Strange sea asymmetry and the NuTeV anomaly

Based on  $R^- = \frac{\sigma(\nu_\mu N \rightarrow \nu_\mu X) - \sigma(\bar{\nu}_\mu N \rightarrow \bar{\nu}_\mu X)}{\sigma(\nu_\mu N \rightarrow \mu^- X) - \sigma(\bar{\nu}_\mu N \rightarrow \mu^+ X)} = g_L^2 - g_R^2 = \frac{1}{2} - \sin^2 \theta_W$

NuTeV obtains  $\sin^2 \theta_W^{\text{NuTeV}} = 0.2277 \pm 0.0016$ ,  $3\sigma$  deviation from previous fits of Standard Model  $\sin^2 \theta_W^{\text{SM}} = 0.2227 \pm 0.0004$ , *i.e.* an anomaly!

**But**, if  $xs(x) \neq x\bar{s}(x)$ :  $\nu s \rightarrow \mu^- c$  and  $\bar{\nu} \bar{s} \rightarrow \mu^+ \bar{c}$  give different  $\sigma$ 's

$\Rightarrow$  shift  $\Delta \sin^2 \theta_W = \int_0^1 dx [xs(x) - x\bar{s}(x)] F(x)$  ( $F(x)$  is NuTeV folding function)

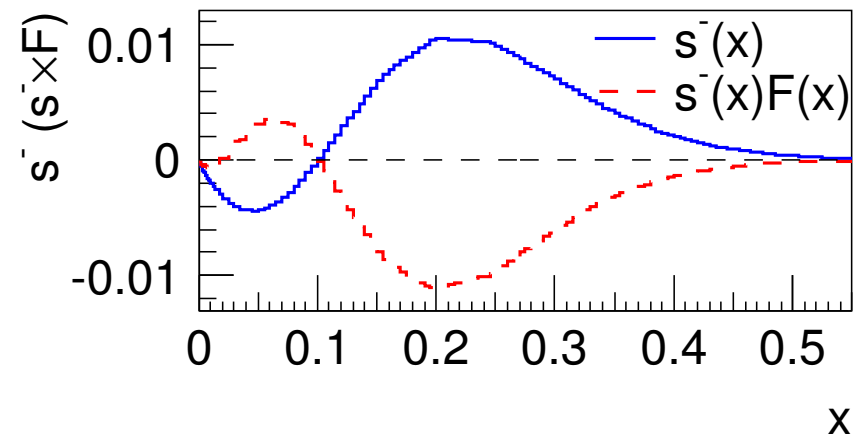
**Our model:**  $0.0010 \leq S^- = \int_0^1 dx [xs(x) - x\bar{s}(x)] \leq 0.0023$  (varying details,  $\sigma_d$ )

$\Rightarrow -0.0024 \leq \Delta \sin^2 \theta_W \leq -0.00097$

*i.e.* discrepancy reduced to  $1.6 - 2.4\sigma$

*Cf.* CTEQ data analysis with similar result (Olness et al., hep-ph/0312323)

*Cf.* perturbative asymmetry opposite but small, hep-ph/0404240

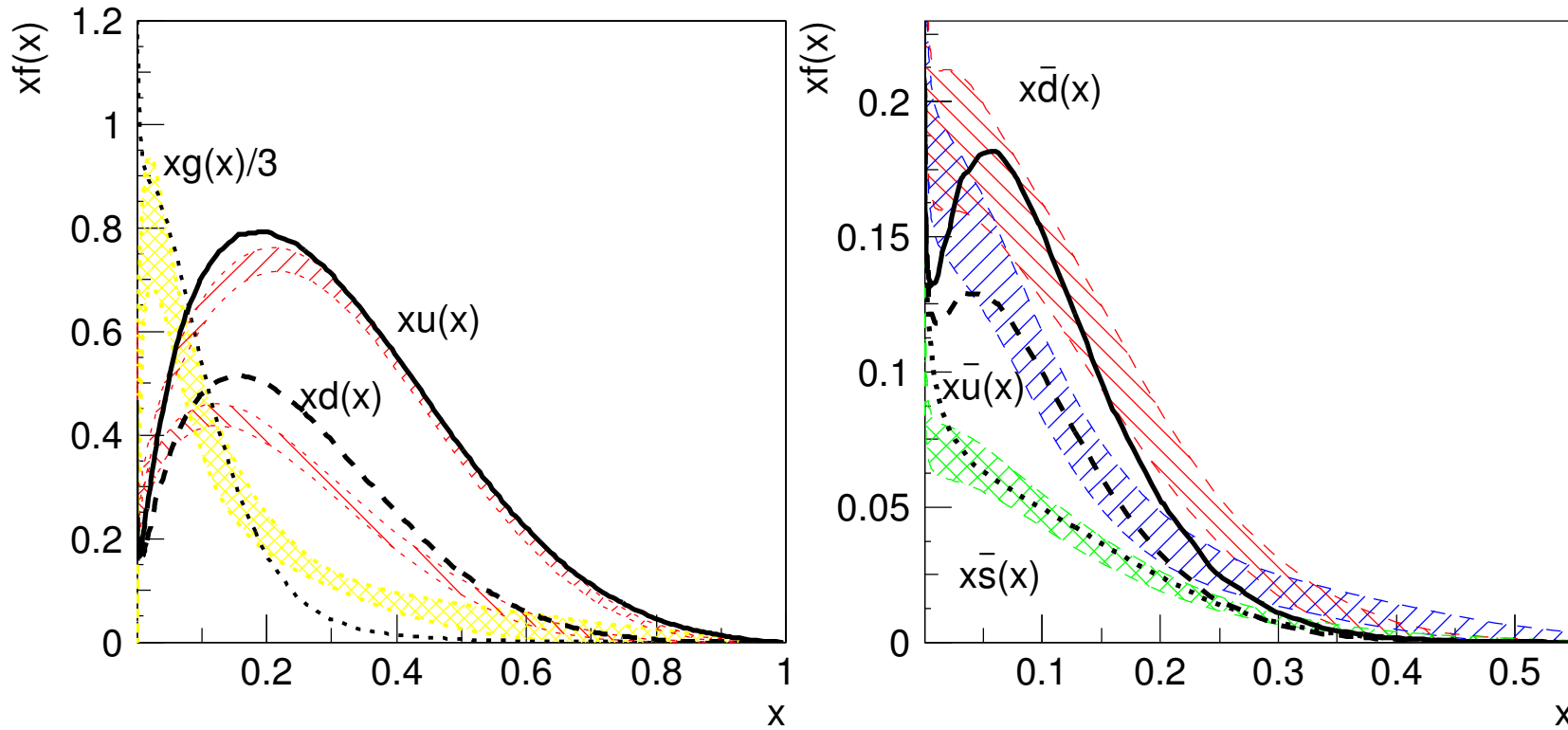


**No significant indication for physics beyond the Standard Model !**

## Comparison with CTEQ6M distributions

CTEQ: “arbitrary” parametrization, 20 shape parameters (+ normalisation)

Our model: physically motivated, 4 shape parameters with reasonable values



$Q = 1.1 \text{ GeV}$

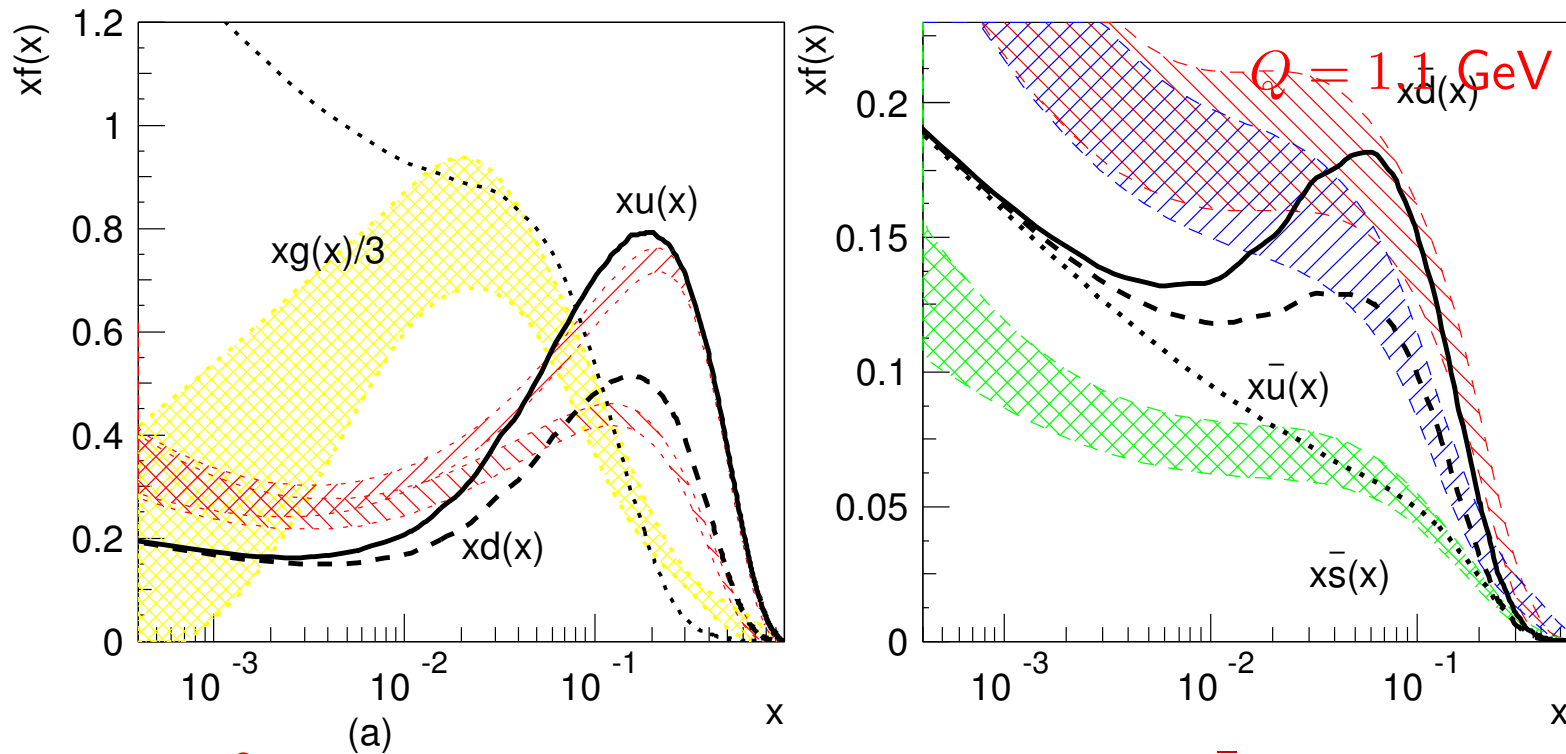
For  $x \gtrsim 10^{-2}$

- valence and sea quarks agree with CTEQ
- gluon lower than CTEQ at large  $x$

## Comparison with CTEQ6M cont.

CTEQ:  $xf(x) \rightarrow x^{-0.3}$  for  $x \rightarrow 0$  at  $Q_0 = 1.3$  GeV

Our model:  $xf(x) \rightarrow 0$  for  $x \rightarrow 0$  at  $Q_0 = 0.75$  GeV



For  $x \lesssim 10^{-2}$ : Gluon larger than CTEQ, but  $u\bar{u}$  and  $d\bar{d}$  sea lower than CTEQ

Large  $xg(x, Q_0^2)$  and low  $Q_0^2$  needed to give low- $x$  quark sea via DGLAP

⇒ Need for additional source of  $q\bar{q}$  without accompanying gluons !?

## Possible source of $q\bar{q}$ : GVDM in $ep$ at low $Q^2$

Quantum fluctuations of photon:

$$|\gamma\rangle = C_0|\gamma_0\rangle + \sum_V \frac{e}{f_V}|V\rangle + \int_{m_0} dm_V(\dots)|V\rangle$$

i.e. photon  $\rightarrow$  vector mesons  $V = \rho^0, \omega, \phi \dots$  + **continuum**

followed by  $Vp \rightarrow X$  with soft hadronic cross-section

$$\sigma_{T,L}^{\text{GVDM}} = P(\gamma \rightarrow V)\sigma_{Vp}; \sigma_{Vp} = A_V s^\epsilon + B_V s^{-\eta}; \epsilon \approx 0.08$$

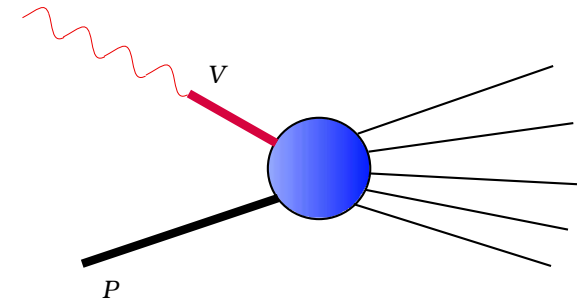
$$s_{\gamma p} = Q^2 \frac{1-x}{x} + m_p^2 \approx Q^2/x \text{ at small-}x$$

$$\Rightarrow F_2^{\text{GVDM}}(x, Q^2) = \frac{(1-x)Q^2}{4\pi^2\alpha} \left\{ \sum_V r_V \left( \frac{m_V^2}{Q^2+m_V^2} \right)^2 \left( 1 + \xi \frac{Q^2}{m_V^2} \right) + r_C \frac{m_0^2}{Q^2+m_0^2} \right\} A \left( \frac{Q^2}{x} \right)^\epsilon$$

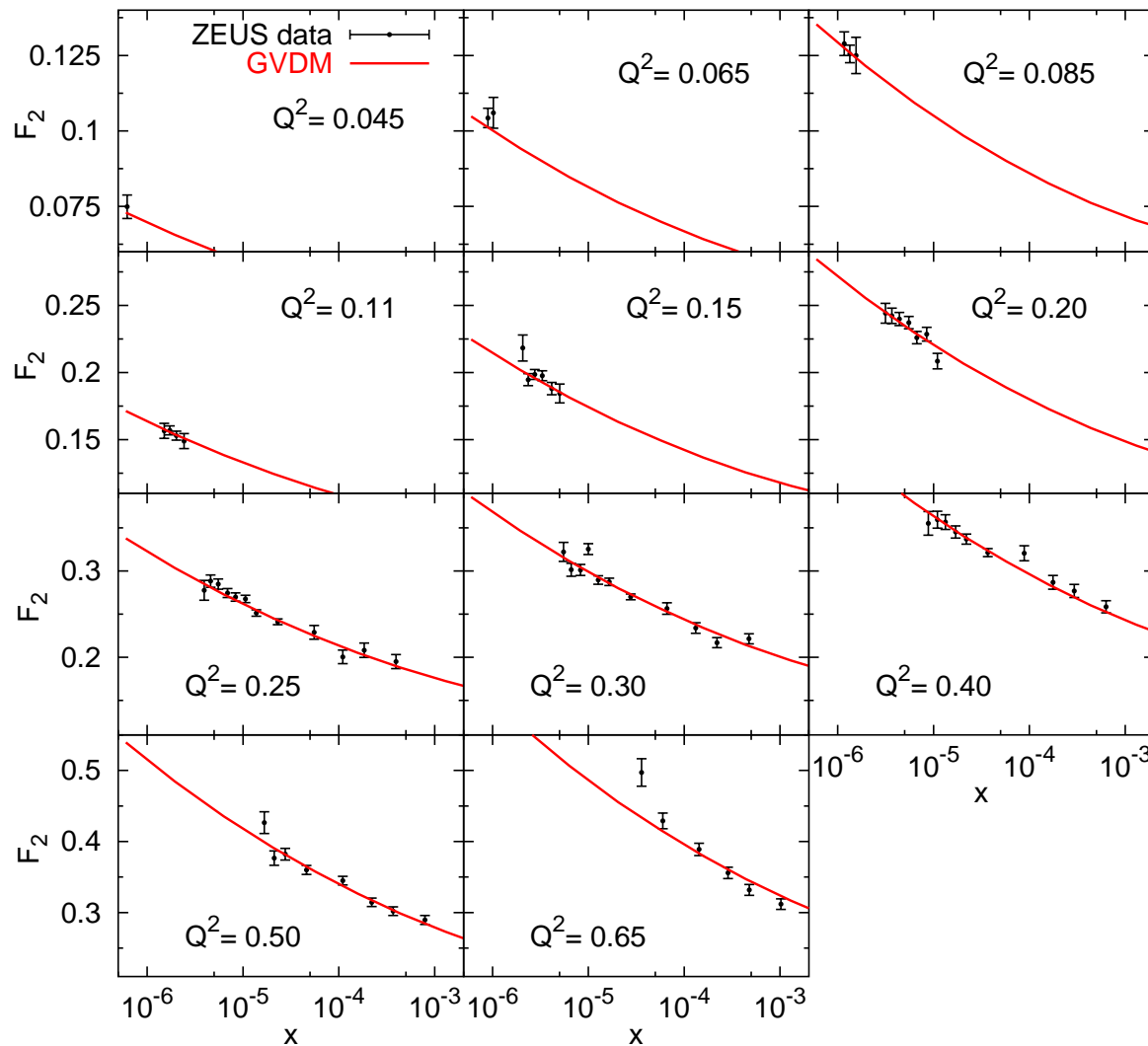
More complex  $Q^2$ -dependence from  $\sigma_L$  and **continuum** than simple VDM

Parameters 'known' from GVDM:  $r_V = \frac{4\pi\alpha}{f_V^2} \frac{A_V}{A}$ ,  $r_C = 1 - \sum_V r_V$

$m_0 \approx 1 \text{ GeV}$ ,  $r_{V=\rho,\omega,\phi,C} = 0.67, 0.062, 0.059, 0.21$ ;  $\xi \approx 0.25$



# HERA $F_2$ at low $Q^2$



ZEUS 1997 data

GVDM model fits well

$$\chi^2 = 87 / (70 - 4) = 1.3$$

with parameter values

$$\epsilon = 0.091$$

$$m_0 = 1.5 \text{ GeV}$$

$$A = 71 \mu\text{b}$$

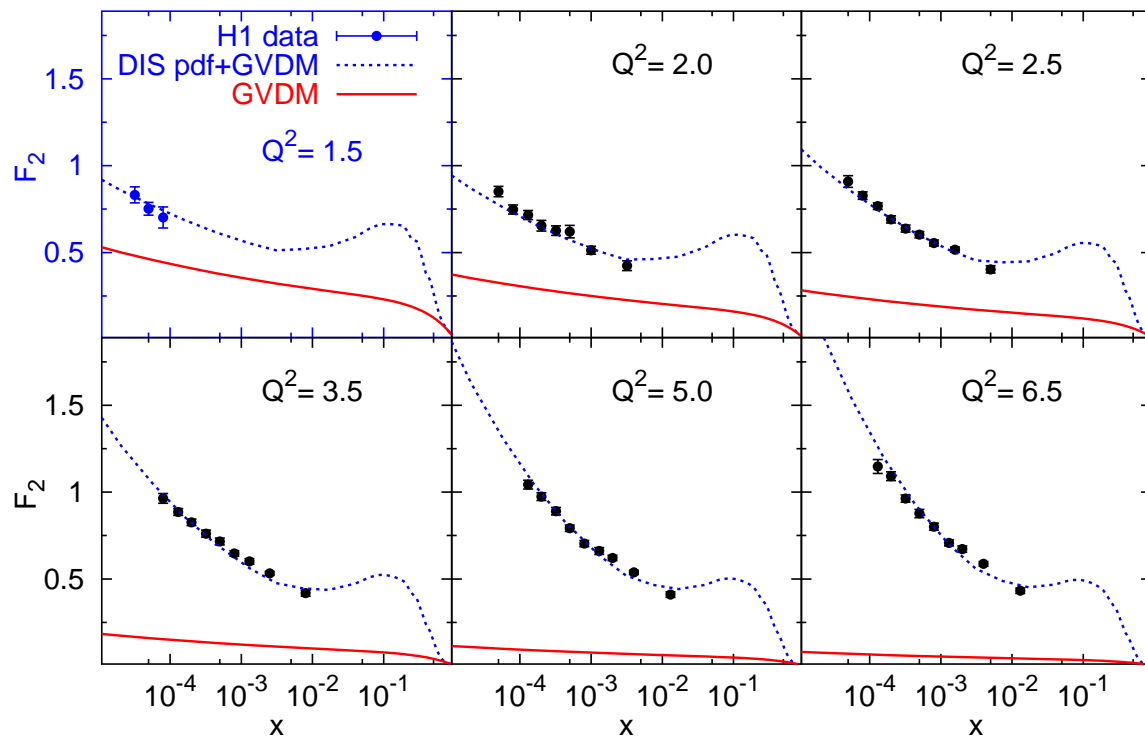
$$\xi = 0.34$$

as expected

For higher  $Q^2$  and  $x$  need parton densities – how to combine?

# HERA $F_2$ at intermediate $Q^2$

Simplest solution: Use GVDM scale-down factor (form factor) for higher  $Q^2$



$$\text{GVDM} \times \left( \frac{Q_0^2}{Q^2} \right)^a \text{ with } a = 1.8$$

for  $Q^2 > Q_0^2 = 1.26$  (fitted)

→ GVDM negligible for  $Q^2 \gtrsim 3$

Adding parton densities,  
here Alwall-Edin-Ingelman model,  
gives good description of data  
without negative gluon density

# Summary

- Our physically motivated model, based on Gaussian momentum fluctuations, gives the  $x$ -shape of parton distribution functions in hadrons  $f_i(x, Q_0^2)$
- Sea quark distributions from hadronic quantum fluctuations, *e.g.*  $|N\pi\rangle$ ,  $|\Lambda K\rangle$
- Nice description of large- $x$  valence quark data  
↔ Gaussian momenta OK → statistical description of non-perturbative dynamics
- $\bar{u} - \bar{d}$  asymmetry in agreement with data  
↔ Meson-baryon fluctuations explain non-perturbative sea
- $s - \bar{s}$  asymmetry sufficient to reduce the NuTeV anomaly below  $2\sigma$   
↔ No hint of new physics
- Valence and sea quarks  $\sim$  CTEQ, but gluon differs !?